Application of the on-line strip triangulation program STRAUS G. Bauer, BSc (Eng) Kombinat VEB Carl Zeiss JENA, GDR Commission III 1. General

For highly accurate photogrammetric single point determination, analytic phototriangulation is generally adopted on a worldwide scale. Highest accuracy is obtained by using the bundle method in connection with analytic plotting instruments or precision comparators (stereo or mono). For provision of control coordinates for photogrammetric stereoplotting the method of independent models is used, too. With this, coordinates can be determined by analog stereo plotters. Use of computer-aided techniques at photogrammentric plotting instruments caused the development of the on-line triangulation method with computer-aided stereoplotting systems. On-line triangulation is a method of measurement and immediate processing of measured values which allows the operator to recognize and eliminate coarse errors and other model mistakes during measuring.

## 2. Concise description of the program package

## 2.1. DZT 90 x 120/RGS instrument configuration

The DZT 90 x 120/RGS computer-aided stereoplotting system of the Kombinat VEB Carl Zeiss JENA can be affiliated to the analog stereoplotting systems (Stereometrograph, Topocart, Stereoplot) as a complementary unit.

Integration of such a system into the processing for graphic mapping alters the restitution technologies. During restitution, the stereo operator has an additional display with keyboard, a double pedal switch and a functional keyboard for control of the automatic drawing. For determination of control marks for graphic, numeric, and photographic interpretation of photographs the on-line strip triangulation program STRAUS is used for the DZT 90 x 120/RGS computer-aided stereo plotting system. This program uses the possibility of the system-internal graphic output.

### 2.2. Program structure

The STRAUS strip triangulation program is for measurement, calculation, and adjustment of aerial triangulation strips. The program is based on the technique of independent models. Primary data (model coordinates) are acquired in relatively oriented photogrammetric models with the DZT 90 x 120/RGS during measurement of a triangulation strip at the stereoplotter. Strip formation is performed after measurement and check of a scale model as well as orientation of the first strip model. Within one strip number of models is not limited. During measuring up to 25 reference points (projection centres, tie points, control points) can be registered within one model. For one triangulation strip up to 40 control points (planimetric, height, and complete control points) can be considered.

Program package STRAUS consists of four part programs. All programs are interlinked via common data files. The part programs are MACHINE, CENTRE, STRIP, and GRID.

### 2.2.1. MACHINE program

This program specifies the kind of the plotting machine used in strip triangulation, the formats for coordinate recording, the admissible errors in double measurements, and parameters for the connection of measuring instruments. After call-up of the program and after every parameter change (possible by simple exchange operation), the current assignments are listed on the display. Before the processing of an aerial triangulation strip the coordinates of the control points have to be stored as a file on the floppy disk.

## 2.2.2. CENTRE program

In aerial triangulation the projection centres are included in the measurement and computation process. For setting the projection centre during the model measurement, special setting marks are used. The coordinate differences between the real projection centres and the setting marks have to be determined by a calibration measurement. This determination of the coordinates of the projection centres is performed by spatial intersections of straight lines. The resulting correction vectors of the setting marks are stored and taken into account during on-line strip triangulation in the measurement of the projection

centres of each model.

The CENTRE program can be called up several times during one strip triangulation.

## 2.2.3. STRIP program

The STRIP program is the measuring and processing program proper for on-line strip triangulation according to the method of independent models. It is subdivided into four subroutines:

- Strip formation
- Absolute strip orientation
- Graphical representation of error vectors
- Calculation of setting elements

### 2.2.3.1 Strip formation

This subroutine serves for the measureemnt and recording of the coordinates of the projection centres, of the tie points and control points in the relatively oriented photogrammetric models. This subroutine performs the strip formation from the individual photogrammetric models at the model scale and in the orientation of the first model of the triangulation strip. After the conclusion of the measurement of each model the other subroutines of STRIP may be called up.

### 2.2.3.2. Absolute orientation

This subroutine transforms the triangulation strip existing at the model scale and in the orientation of the first model of the strip into the ground coordinate system (control points). After the rigorous spatial Helmert transformation the residual errors at the control points in the ground coordinate system are indicated on the display. The residual errors are also used for selecting the variant of strip adjustment according to independent polynomials for each coordinate. The following variants of strip adjustment are available:

- without adjustment
- planimetric adjustment
- height adjustment
- planimetric and height adjustment

Following approaches were chosen as polynomials for strip adjustment:

 $X = a_0 + a_1 x + a_2 y + a_3 x^2 + a_4 xy$   $Y = b_0 + b_1 x + b_2 y + b_3 x^2 + b_4 xy$  $Z = c_0 + c_1 x + c_2 y + c_3 x^2 + c_4 xy$ 

After strip adjustment the residual error at the control points are indicated on the display, then all strip points are transformed fron the model coordinate system into the ground coordinate system. The subroutine "absolute orientation" can be called up repeatedly.

# 2.2.3.3. Graphical representation of error vectors at the control points

The residual errors obtained according to the chosen variant of strip adjustment are represented by this subroutine at a freely selectable scale (control points and residual errors) on the plotting table. Using this error vector representation the operator may choose a different variant of strip adjustment aftre absolute orientation. Following the kinds of representation:

control points
control points and projection centres
control points, projection centres and tie points

## 2.2.3.4. Calculations of setting values

With this subroutine the setting values of the orientation elements and basic components are calculated for a chosen model scale for subsequent plotting of the photographs of the triangulation strip at analog plotters. The subroutine performs a computational absolute orientation of each model of the point coordinates stored during strip measurement to the identical points of the adjusted strip coordinates. The corrections for the orientation elements and base components are applied to the values stored during the dialog of the strip formation routine.

## 2.2.2. GRID program

With this program ground control data can be obtained for subsequent plotting. A choice can be made between a grid of lines and a grid of crosses. The scale, size, line spacing, lettering, etc. are input via dialog.

## 3. Technology of on-line strip triangulation

Nowadays, aerial triangulation is one of the routine jobs of photogrammetric departments. Working in technological steps is quite essential for this kind of task.

### 3.1. Project preparation

It is useful to prepare the project for each aerial triangulation to be carried out. In our case, project preparation means processing of already existing photographic material for measurement in the plotter. The preceding technological steps photo flight planning and signalling project are not included. Proper project preparation can speed up measurement of the photographic material in the plotter. The main steps are:

- Transformation of photo centres from the photo material onto the project map with the aid of contoures
- Marking of the required map sheet (processing area) in
- the projection map
- Selection and transformation of control points (signalled points or contour points or map control points) in the

projection map. Number of control points depends on number of models. The individual departments, i.e. the aerial triangulation programs they use have respective normatives. For arrangement of control points, special configurations have to be observed.

- Selection of tie points from model to model and strip to strip on the base of the photographs and their transformation in the project map.
- Preparation of a "technical design" of aerial triangulation.
   The technical design is a tracing of the data of the project map.

Following data should be included:

- borders of the processing area
- map sheet sections
- all image numbers
- all planimetric and height points
- all model tie points
- additional information such as object designation, scale, camera used, etc.

The technical design is required for point transformation and measurement.

## 3.2. Point transformation

For aerial triangulation, signalled control points, contour marks, or arbitrarily marked points can be used as model tie points. During project preparation, the areas for the position of the tie points are selected and marked on the basis of the photo material. Highest accuracy of point identification during measurement is acquired by the signalled points. Signalling, however, requires great efford before the flight as well as high demands on the photo flight navigation. The use of clearly defined contour marks is much more efficient. These points are selected at a mirror stereoscope and marked in paper copies. Additionally, it should be useful to make sketches for quicker identification of the marks during measurement.

Accuracy depends on the quality of contour point definition. In build-up areas, this quality nearly corresponds to that of the signalled points. When using the arbitrarily marked points, they are marked with a stereoscopic laser point marker (e.g. with TRANSMARK) in the predefined areas. Very good accuracy is acquired if setting errors and machine faults of the point marker are avoided.

#### 3.3. Measurement

For measurement of aerial triangulation strips, adaptation of the stereo plotters of Kombinat VEB Carl Zeiss JENA by special devices is not necessary.

The control point coordinates under project designation being entered and stored, connection to measuring instrument, error limits and further declarationss are determined in the MACHINE program.

Prior to measurement of an aerial triangulation strip the coordinates or correction vectors, resp., for the projection centres should be determined with CENTRE program. This determined nation can be easily done. Due to the various designs of the stereoplotters, there exist different measuring positions for the different calibrated principal distances.

Calibration marks on the mark plates

can be used as auxiliary means of setting. For this purpose, set and register the marks in the right and the left image with a great and a small projection distance in monocular mode. The measurement concluded, the mean measured values in succession, the calculated correction vectors, and the base components are output on the terminal or on the printer. Confirmation of the measurement is followed by storage of the correction vectors for the projection centres. For the actual strip triangulation, beside the photographs the technical design is used at the stereo plotter. It comprises all data required for measuring the stereo models - strip designation, image numbers for model designation, designations for control and tie points. If possible, carry out formation of all models of a triangulation strip with a constant base setting."Mean base" can be determined during preparation. Prior to actual measurement, enter orientation data and base components according to the relative orientation of the photogrammetric model via dialog. These values are stored in a file for calculation of setting values.

Measurement of each model is performed in a coordinate system defined by the projection centres. The coordinates are corrected by the correction vectors. Before registration of each point enter the respective designation via dialog. After measurement of the second and each following model of a strip residual errors of the model connection in model scale are indicated in the display. On the basis of these data the evaluator can accept the model connection and proceed measurement with processing of a further model, output the results via printer, or change them.

During modification there exists the possibility of erasing points or substitution by single measurements or measurement of the entire last measured model. Then the residual error is indicated again. In case of incorrect double measurements (error limit specified in MACHINE program) error indication is performed, measurements of the respective points are eliminated and have to be performed anew. After measurement of each model you can call up the other part programs (2.2.3.2., 2.2.3.3., 2.2.3.4.).

During absolute orientation of the aerial triangulation strip the strip coordinates in model scale of the model measured first are transformed in the control point coordinate system. Residual errors at the control points in the State plane coordinate system are indicated on the display.

Thus, you have the additional possibility to adjust the strip (see 2.2.3.2.).

After this transformation allstrip coordinates are transformed in State plane coordinates with the correction polynomes determined during adjustment. The coordinates stored on file can be directly used as control point file for computer-aided stereoplotting or for map sheet preparation (2.2.4.).

Graphic representation of the error vectors is an auxiliary means for evaluation of residual errors for the selection of the mode of strip adjustment. The subroutine calculation of setting elements is for calculation, display, and output via printer of setting values for a desired model scale.

## 4. Results

The STRAUS on-line strip triangulation program has been wellproved in several photogrammetric departments for most differnt cases of application. All users appreciate the useroriented dialog, easy program handling and high efficiency by quick on-line testing of the results. Representing the various fields of application, we wish to make you acquainted with the program utilisation for photogram-

make you acquainted with the program utilisation for photogram metric control point determination in open cast surveying. In most lignite open casts in the GDR calculation of cubic contents as well as mining engineering safety control are

performed by methods of aerial photograph plotting. For this purpose, control points have to be determined in each model. Generally, control points of an open cast are permanently

signalled and determined in geodetic terms. In Winter, several persons are required immediately before the photoflight to hold the respective signals for each model visible from above. For one year now we have been using the STRAUS on-line strip triangulation program in the DZT 90 x 120/RGS computer-aided stereoplotting system for control point determination during winter.

Average strip length for the open casts is 5 to 7 models. An accuracy of m'xy=25µm and m'z=12µm is acquired with wideangle photographs and a scale of abt. 1 : 9000. Exclusively unsignalled terrain points are used as model tie points. Results are improved by using arbitrarily marked tie points (e.g. with TRANSMARK). The accuracies acquired that way are sufficient for the purpose of stereoscopic model restitution (graphic and digital) for mass determination and mining engineering safety control. Signalled points geometrically spread over

the entire open cast served as control marks. For strip adjustment, 2 points at each the strip beginning, middle, and end are used. Using the STRAUS on-line strip triangulation program for control point determination in GDR lignite open casts during Winter saves cost and manpower. Performing the triangulation requires 20...30 min/model on average.

Table 1. Printout. Determination of the setting elements (strip, model

scale, model) STREIFEN: STREIFEN.1 MODELLMASZSTAB = 1:12500MODELL: 156-158 BX = 169.100 MMBY = 28,998 MMBZ = 30.463 MMPHIL = 11.688PHIR = 11.488OMEL = 8.760 OMER = 8.930KAPL = 4.600KAPR = 4.450MODELL: 158-160 BX = 184.072 MMBY = 28.960 MMBZ = 28.149 MMPHIR = 11.904PHIL = 11.884 OMEL = 8.568OMER = 7.748KAPL = 3.400KAPR = 6.800MODELL: 160-162 BX = 188.346 MMBY = 28.685 MMBZ = 29.712 MMPHIL = 11.870PHIR = 12.120OMÉL = 9.308 OMER = 8.328KAPL = 3.200KAPR = 0.350MODELL: 162-164 BX = 186.137 MMBY = 34.582 MMBZ = 30.016 MMPHIL = 11.656 PHIR = 11.316OMEL = 10.329OMER = 10.409KAPL = -0.250KAPR = 0.300MODELL: 164-166 BX = 186.962 MMBY = 33.035 MMBZ = 29.550 MMPHIL = 12.013PHIR = 12.343OMEL = 10.328OMER = 10.728KAPL = 1.700KAPR = 0.300MODELL: 166-168 BX = 185.262 MMBY = 33.403 MMBZ = 29.940 MMPHIL = 11.704PHIR = 10.874OMEL = 9.990 OMER = 10.860KAPL = 1.900KAPR = 3.900