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### Abstract

In digital close range photogrammetry the data flow in data preprocessing and data analysis should be fully automated to have the most profit of the digital data acquisition for example by the use of CCD-sensors.

In order to realize this idea sequential algorithmization must be performed considering problems such as data compression, filtering, edge detection, image matching, bundle block adjustment and object reconstruction. The paper discusses the use of tuned systems in data preprocessing, heuristic procedures in image matching and the integration of object reconstruction into bundle block adjustment.

The reconstruction of a cube demonstrates the application of the methods proposed.

### 1. Introduction

With the use of CCD-sensors close range photogrammetry can be fully automated. This implicates a chain of algorithms ranging from sensor calibration to object reconstruction (A. Grün, 1987). Especially with regard to real-time applications the algorithmization should be fast and robust using adequate hardware architecture such as image processors and most recently transputers.

Although camera calibration remains an object to be investigated furthermore in detail (H.A. Beyer, 1987, R. Lenz/D. Fritsch, 1988) main interest of photogrammetrists is directed to the data flow in data preprocessing and data analysis. Data preprocessing should contain mainly grey value manipulation whereas in data analysis grey value evaluation predominates.

Some methods on both steps will be demonstrated by the following task: reconstruct a cube of 20 (cm) side length by means of three digital (synthetic) images generated by a CCD-sensor of 245 H x 319 V picture elements and with a focal length  $c=15$  (mm). First results have been given by D. Fritsch/G. Strunz (1987) using edge information only; thus the methods applicated and the complete results will be reviewed in the following.

### 2. Data Preprocessing

In data preprocessing some steps have to be performed to lead the digital images (digigrams) to the final data analysis. Above all the pre-

processing must be fast which can be guaranteed by operators with short point spread functions.

Let be

$$y(m,n) = \Phi(x(m,n)) \quad \forall m=0,1,2,\dots,M-1 \quad (1)$$

$$n=0,1,2,\dots,N-1$$

in which  $\Phi$  characterizes the system being used for the preprocessing. Its design may result from heuristic and analytic procedures respectively, depending on the problem to be solved.

With the use of linear time invariant systems in data preprocessing the grey value manipulation is represented by the convolution

$$y(m,n) = \sum_{k=0}^{K-1} \sum_{l=0}^{L-1} h(k,l)x(m-k,n-l) = h(m,n)*x(m,n) \quad (2)$$

whereby  $h(k,l)$  is the 'kernel' (point spread function or impulse response) of the system being applied. Some experience has shown that the length  $K$  and  $L$  of the kernel should not be greater than 5 for many manipulations of the data. To provide for linear phase it is recommended to use operators with  $K$  and  $L$  odd resulting into

$$y(m,n) = \sum_{k=-(K-1)/2}^{(K-1)/2} \sum_{l=-(L-1)/2}^{(L-1)/2} h(k,l)x(m-k,n-l) \quad (3)$$

otherwise the preprocessed pixel  $y(m,n)$  is not defined at the original location of  $x(m,n)$  but shifted  $\pm m/2$  and  $\pm n/2$  respectively.

For the computation of the kernel  $h(k,l)$  frequency considerations are often helpful and, in some cases, necessary. Especially, when using selective systems (D. Fritsch, 1984) like filters, noise eliminators, contrast amplifiers etc. the impulse response has to take care for precise geometry. For that reason a comprehensive program package is used in our application in which a quadratic programming algorithm provides for sub  $l_{\infty}$  approximations within the frequency domain (D. Fritsch, 1987, 1988). The following example demonstrates the optimization strategy:

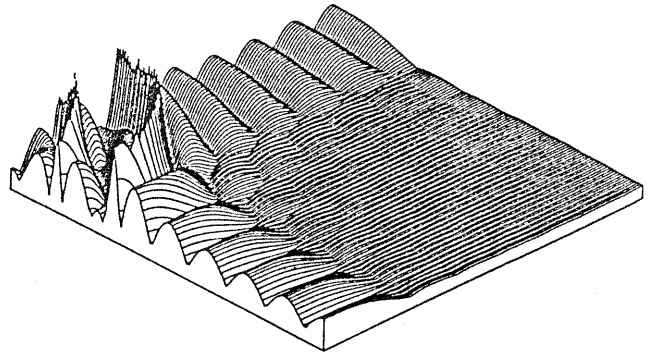
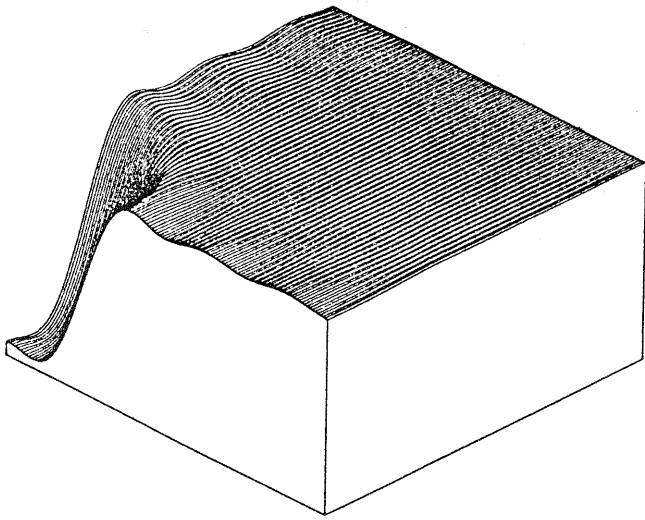
Design a circular shaped amplifying highpass with  $K=L=15$  as well as stop- and passband frequencies  $w_s=0.07\pi$ ,  $w_p=0.16\pi$  within  $w \in (0.,0.5\pi)$ . The approximation should make use of 14400 sample points within the frequency domain.

In Fig. 1 the results of a least squares approximation and a sub  $l_{\infty}$  approximation are represented. While the least squares residuals (b) amount to maximum values of  $\max(v_i)=0.104$  leading to a shifted geometry of about 10%, the optimized frequency response (c) has only  $\max(v_i)=0.07$  reducing the error behaviour (d) to 7%. Thus it is important to tune the systems such that the errors one has to pay for in data preprocessing are kept to minimum.

In order to detect the edges of a digigram a differentiator must be applied to provide for the gradient of the image. Among well-known dif-

(a)

(b)



(c)

(d)

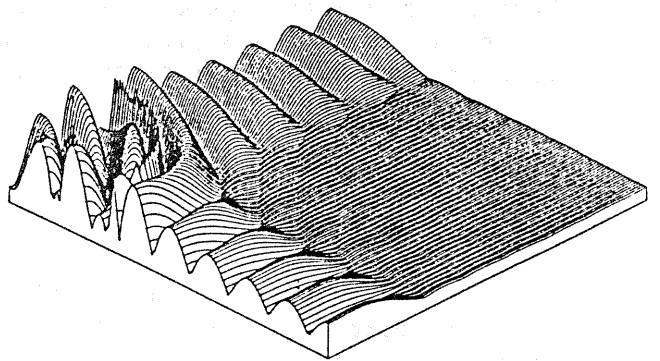
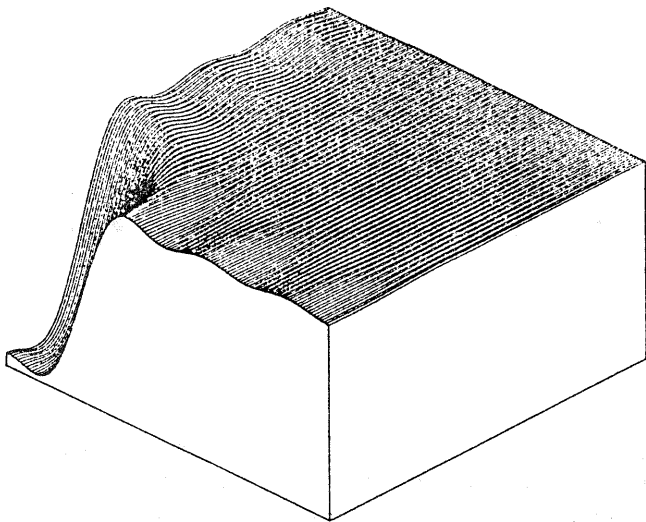


Fig. 1: Design of a circular shaped amplifying highpass  
(a) least squares frequency response  
(b) least squares residuals (Dim: db)  
(c) sub  $l_\infty$  frequency response  
(d) sub  $l_\infty$  residuals (Dim: db)

differentiator templates in digital image processing the question arises, which operator can be used in digital photogrammetry and of which length should its impulse response be.

A comparison between a simple analytical (3x3) operator, the heuristic Sobel operator and a designed (5x5) operator (D. Fritsch, 1987) gives advantages for the benefit of short (3x3) operators. The operators used can be seen in Fig. 2.

(a) simple analytical

$$\begin{bmatrix} 0 & -1/2 & 0 \\ 0 & 0 & 0 \\ 0 & 1/2 & 0 \end{bmatrix} \quad \begin{bmatrix} 0 & 0 & 0 \\ -1/2 & 0 & 1/2 \\ 0 & 0 & 0 \end{bmatrix}$$

(b) Sobel operator

$$\begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix} \quad \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

(c) Design by means of the REMEZ algorithm

$$\begin{aligned} h(-2) &= -0.1042030 = -h(2) \\ h(-1) &= 0.2212293 = -h(1) \\ h(0) &= 0.0 \end{aligned}$$

Fig. 2: Differentiator templates

Particularly with regard to the vectorization of the image gradient it is better to have a smaller bandwidth of pixels representing an edge than to work with more coefficients within the differentiator leading to more emphasized edges.

### 3. Data Analysis

The data analysis in digital close range photogrammetry is consisting of image matching, point determination and object reconstruction. The integration of these steps is most recently topic of contributions on digital photogrammetry (B. Wrobel, 1987, H. Ebner et al., 1987). But regarding close range applications it is more appropriate using fast methods (S.F. El Hakim, 1986, H. Haggreen, 1987) leading to heuristic procedures which may depend on the problem to be solved. This implicates for image matching not to use image correlation and least squares matching respectively, but to apply robust procedures detecting target locations and to solve target matching.

#### 3.1 Image matching

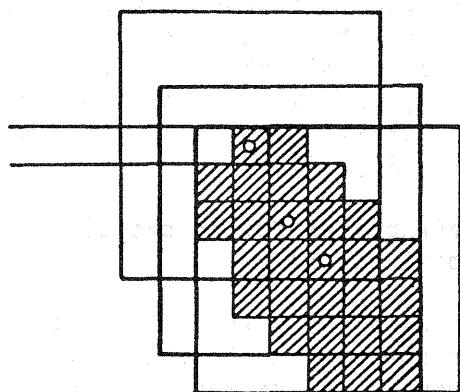
The procedures for fast target location mostly depend on the target pattern. When circular targets are used two main strategies lead to the center of targets

- (i) estimation of the center of gravity
- (ii) calculation of best-fit ellipses within the original image or the image gradient

But first of all, targets must be located automatically. For that reason some operators can be used to search for a target pattern represented by a grey value mountain and valley respectively. For the example below the following operators are used within the convolution (3)

$$h = \frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, \quad h = \frac{1}{5} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \end{bmatrix} \quad (4)$$

both kernels are capable to reduce the noise level on the targets if any. The final centering may be supported by a recursion algorithm using a window of  $n \times n$  in which for each recursion  $k=1,2,\dots,K$  the center is computed. This value has to be compared with the proceeding center; if



to be compared with the proceeding center; if

$$m_K, n_K - m_{K-1}, n_{K-1} \leq 1 \text{ pixel} \quad (5)$$

the optimum center is found (see Fig. 3).

Fig. 3: Window centering

In some cases the center calculation is not satisfactory because changes of imaging conditions cause variable results. For that reason it is more reliable to compute real ellipse centers (G. Zhou, 1986). In our application best-fit ellipses are derived from the constraint

$$a(x_i - x_0)^2 + 2b(x_i - x_0)(y_i - y_0) + c(y_i - y_0)^2 = 1 \quad \forall i=1,2,\dots \quad (6)$$

whereby  $x_i, y_i$  represents the pixel location at the corner of the ellipse being computed. The parameters  $a, b, c$  as well as the exact position  $x_0, y_0$  are obtained by a least squares parameter estimation using the center coordinates as approximate values. Another strategy for the derivation of ellipse centers is to find two diameters and then calculate their intersection which is the center of the ellipse; but this will not be commented on in the paper.

The target matching problem may be solved using the collinearity equations or the coplanarity condition. Each point in one image (master) has to be matched with its corresponding point taken by another camera (slave image). Using known exterior orientation parameters the result is a straight line (epipolar line)

$$y = ax + b \quad (7)$$

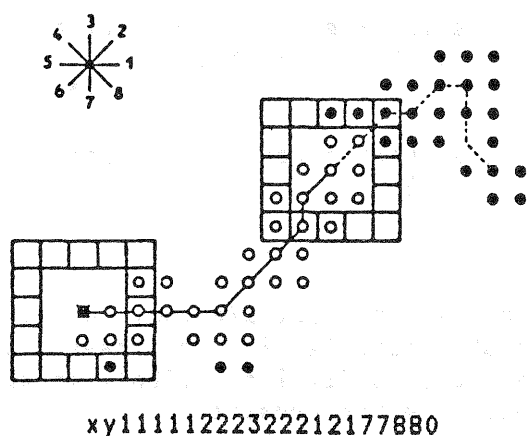
in which the parameters  $a$  and  $b$  are given by the image perspectives. All coordinates of the slave image can be introduced into (7) and compared with a threshold  $\Delta_T$ . If

$$\Delta = \frac{ax}{2} + \frac{b-y}{2} \leq \Delta_T \quad (8)$$

the points match each other. Occasionally more than one target will satisfy (8) therefore the strategy may be reversed to match a point in the slave image with its corresponding point in the master image.

### 3.2 Line Following and Vectorization

The concepts of line following are also very important in digital close range photogrammetry, in particular, when simple objects have to be observed. For example a cube or rhomboid can be reconstructed simply by the use of its corners, whose image coordinates are to determine by line following and simultaneous vectorization within the image gradients. One strategy for line following which is very robust and easy to implement is based on FREEMAN chains (U. Rösler, 1982). Its principle is as follows (Fig. 4):



- (0) define a window of  $m \times m$  at a point  $p(x,y)$
- (1) compare the pixels within the window with a threshold  $\Delta_F$  and compute the center of gravity
- (2) store the pixels representing the edge within the window and delete all grey values
- (3) move the window toward the center of gravity and store the FREEMAN number
- (4) proceed with (1)

Fig. 4: Line following

Thus, the window can move along eight possible directions each representing a so-called 'FREEMAN number'. These numbers may also be used for vectorization but in precise applications it is better that all pixels representing an edge contribute to a polynomial approximation. Appropriate functionals solving the approximation problem are splines, however, for simple objects best-fit straight lines are mostly sufficient.

### 3.3 Combined Point Determination and Object Reconstruction

From the image coordinates the position of points in object space can be derived by bundle block adjustment. Nevertheless, to define the datum parameters or, moreover, to improve the accuracy and reliability of the results and to increase the economy of point determination non-photogrammetric information should be used. General control information, e.g. slope distances, spatial angles and directions, elevation differences, points on a plumb line or any information about the object can be in-

cluded in a combined adjustment with all available data (H. Ebner, 1984) Especially in close range applications, information about the shape or surface of the object is often given. This can be in form of an analytical description, e.g. by a mathematical function. For complex structures digital surface models can be used to describe the form of the object.

At the Chair of Photogrammetry of the Technical University of Munich a program system for combined point determination has been developed which allows for the introduction of various types of non-photogrammetric information (F.Müller/G. Strunz, 1987). This program system is used in our application.

Because the example below deals with a cube, a best-fit cube of length  $a$  is simply to be calculated by the condition equations

$$\left( (X_k - X_i)^2 + (Y_k - Y_i)^2 + (Z_k - Z_i)^2 \right)^{1/2} =: |\vec{P}_i \vec{P}_k| = a \quad (9a)$$

$$\alpha = \cos^{-1} \frac{|\vec{P}_i \vec{P}_j| \cdot |\vec{P}_i \vec{P}_k|}{|\vec{P}_j \vec{P}_k|} =: \pi/2 \quad (9b)$$

whereby  $P_i(X_i, Y_i, Z_i)$ ,  $P_j(X_j, Y_j, Z_j)$  and  $P_k(X_k, Y_k, Z_k)$  are corners of the cube. Their spatial coordinates can be estimated using its image coordinates which result from line following and vectorization, or by the use of targets in an approximation afterwards.

#### 4. Example

In order to demonstrate the methods above a simple example is treated: reconstruct a cube of 20 (cm) side length by means of three digital images within one quadrant (see Fig. 5). The synthetic CCD cameras used

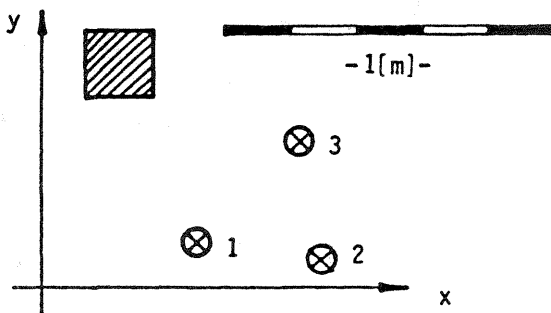
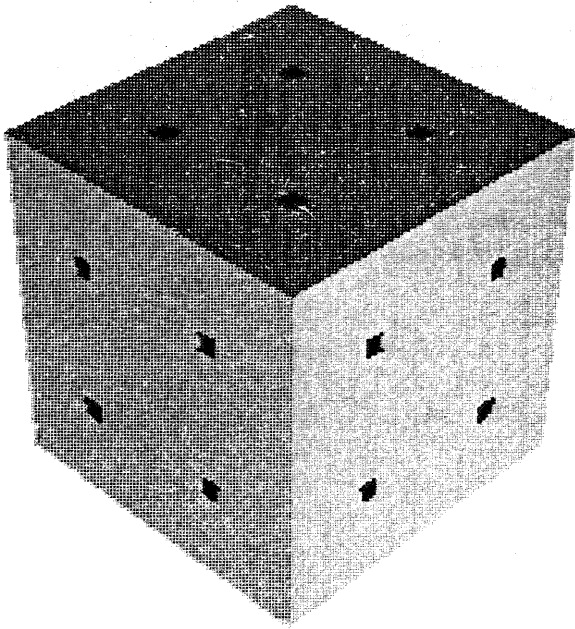


Fig. 5: Location of the (synthetic) CCD cameras

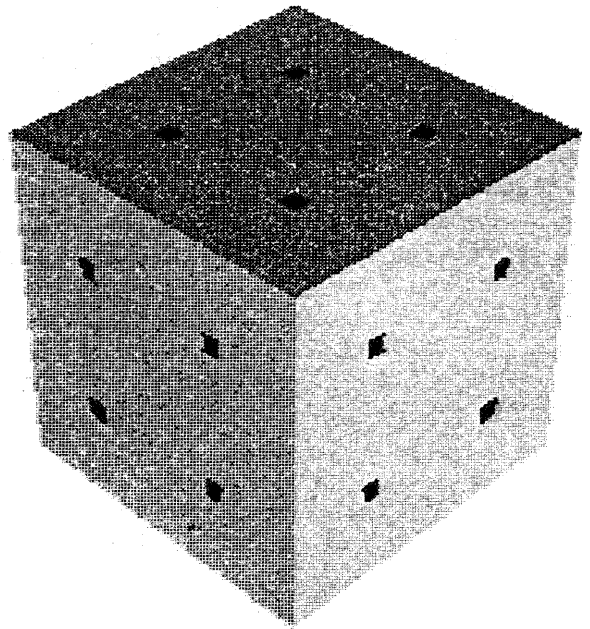
should have a resolution of 245 H x 319 V picture elements; the size of the digital image should be 6.6 x 8.6 (mm) leading to a pixel size of about 0.027 (mm). For that reason three synthetic digital images have been generated for a focal length  $c=15$  (mm) and the premise of known camera positions. In order to study the effect of noise the images were blurred by different SNR of 1%, 5% and 10%. The images taken from position (2) are visualized by Fig. 6, whereas Fig. 7 represents the images taken from the three standpoints but already processed by target location algorithms.

The problem of noise reduction is already treated in D. Fritsch/G. Strunz (1987) and should not be concerned in the following, thus the data preprocessing is restricted on a visual comparison of the differentiators introduced.

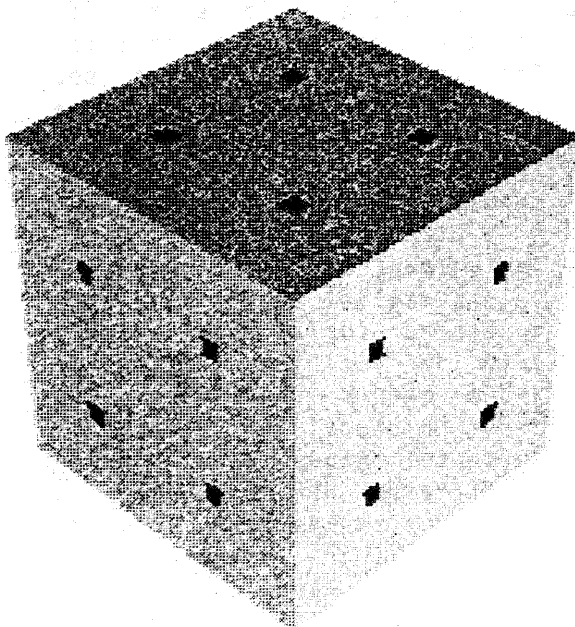
(a) 0% SNR



(b) 1% SNR



(c) 5% SNR



(d) 10% SNR

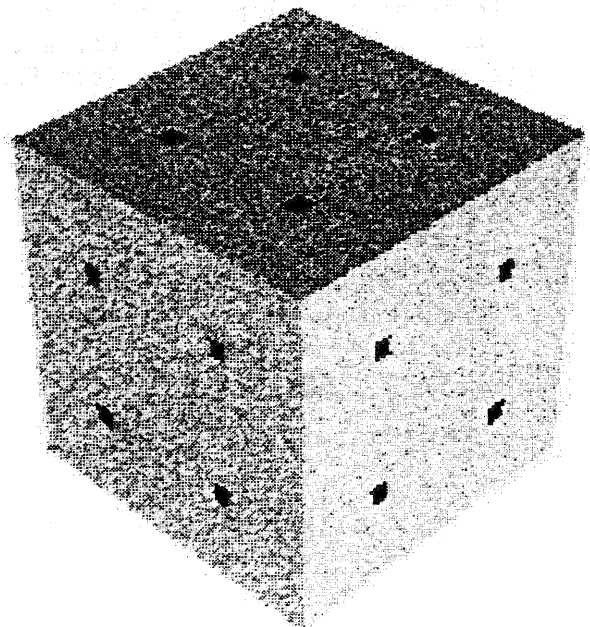
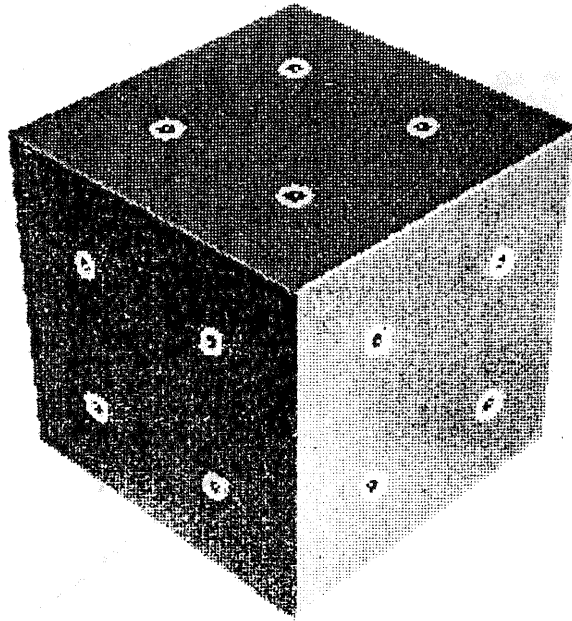


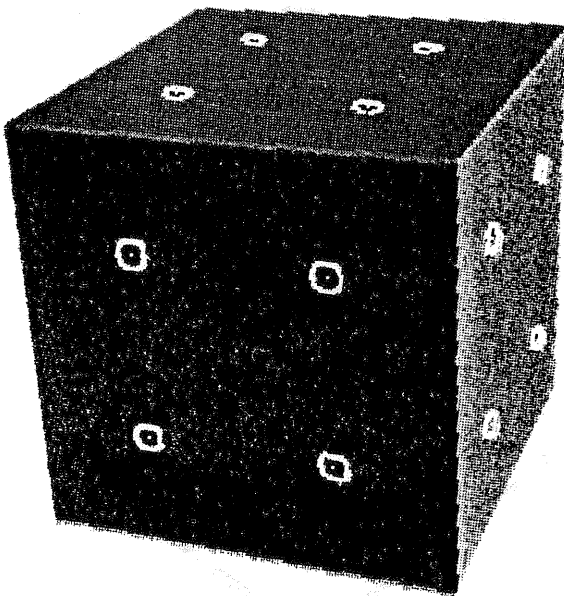
Fig. 6: Digital image at point 2 with 0, 1, 5 and 10% SNR



position (2)



position (1)



position (3)

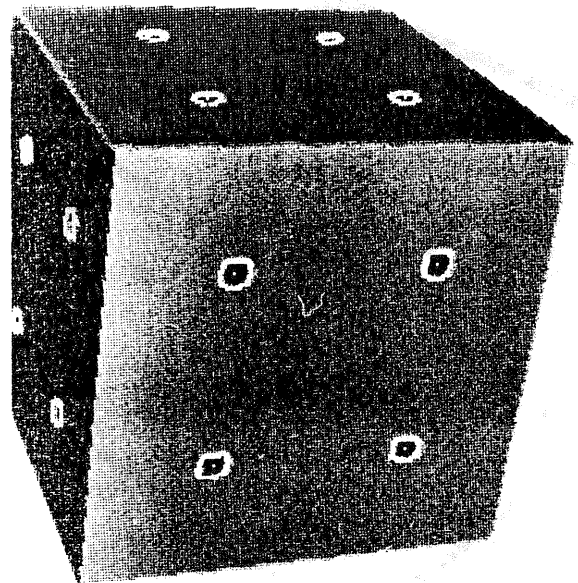
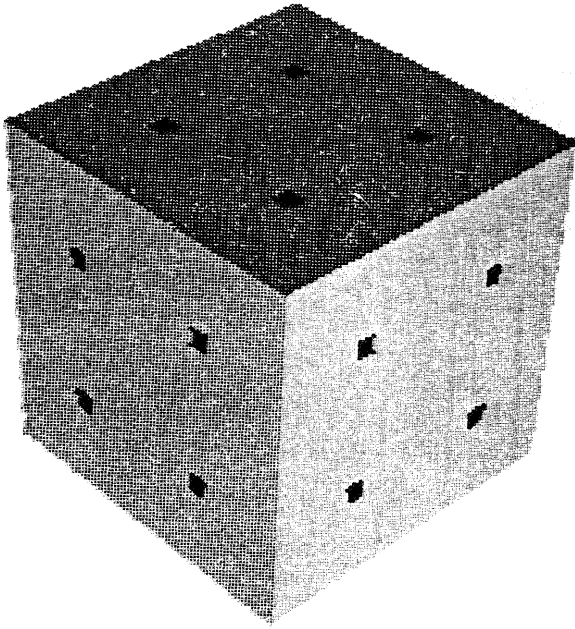
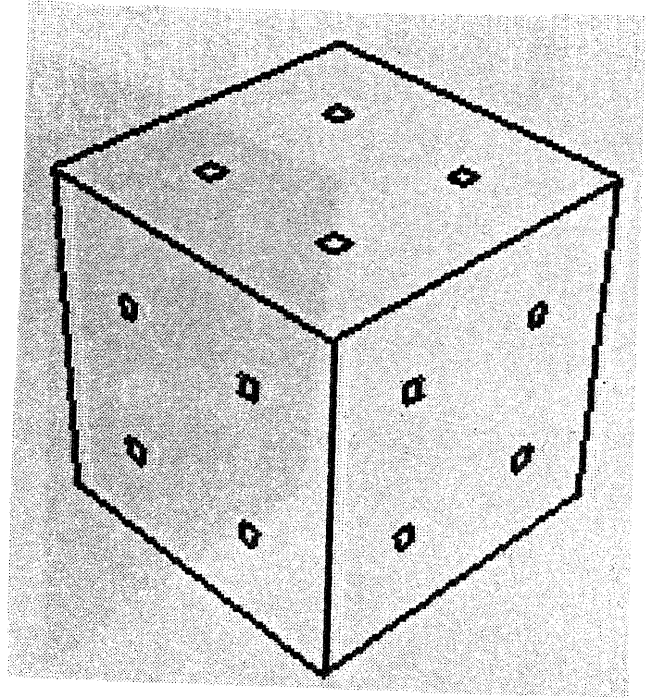


Fig. 7: Digital images with best-fit ellipses (0% SNR)

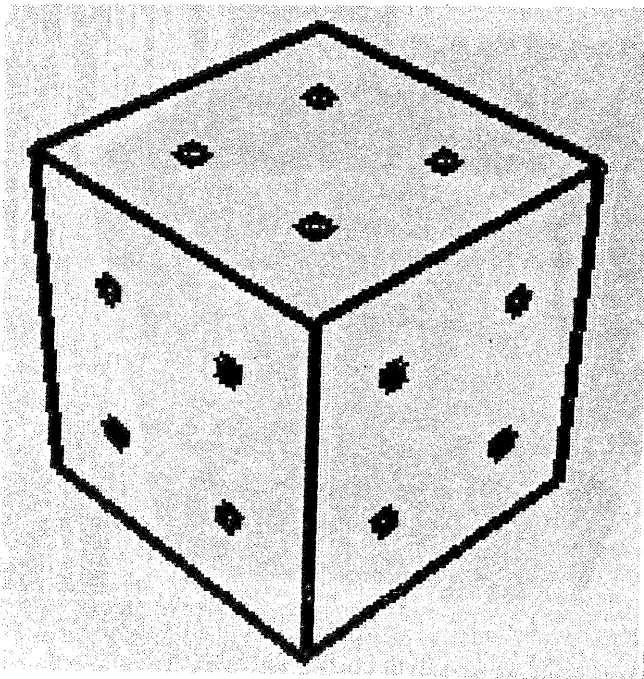
(a) original image  
0% SNR



(b) 3x3 differentiator



(c) 5x5 differentiator



(d) Sobel differentiator

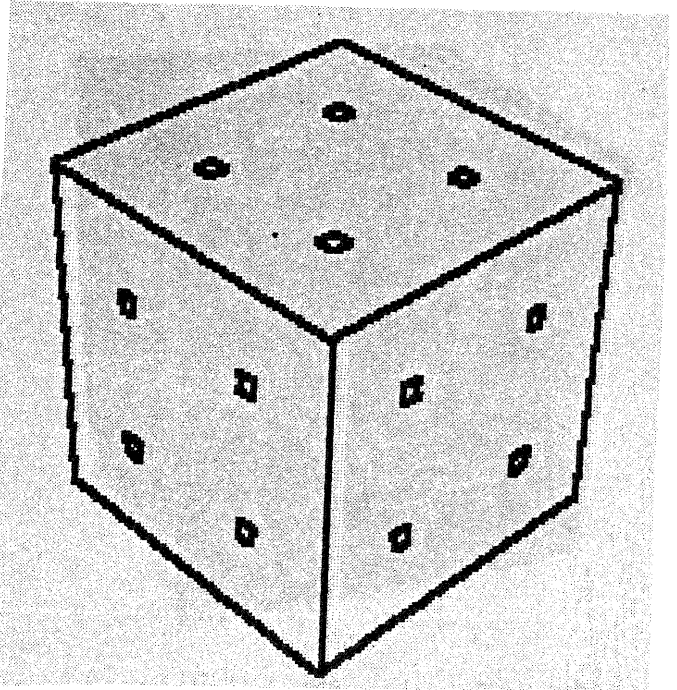


Fig. 8: Image gradients by means of differentiators

For the reconstruction of the cube two strategies are compared with each other: the first one using the image coordinates of the targets and the second one using the image coordinates of corners of the cube. This implicates the algorithmization given by Table 1, in which both the original images and the image gradients are used.

Table 1: Algorithms to reconstruct the cube

step	target information	line information
1	target location by means of convolution operators	vectorization by means of FREEMAN chains and best-fit straight lines (s.l.)
2	calculation of image coordinates of the targets (centers and best-fit ellipses)	calculation of image coordinates of the corners by means of intersections of s.l.
3	image matching using the master and its slaves	image matching using the master and its slaves
4	point determination by bundle block adjustment	point determination by bundle block adjustment
5	best-fit planes, intersection of straight lines and calculation of a best-fit cube	calculation of a best-fit cube

All steps above have been solved by the computer, thus sequential realization leads to an automated data flow in this application.

The cube is reconstructed under different SNR; its side length and corresponding standard deviation can be found in Table 2.

Table 2: Reconstruction of the cube

SNR (%)	target information		line information	
	$\hat{a}$ (cm)	$\hat{\sigma}_a$	$\hat{a}$ (cm)	$\hat{\sigma}_a$
0	19.989	0.023	20.128	0.027
1	19.990	0.030	20.131	0.029
5	19.991	0.043	20.132	0.032
10	19.977	0.054	20.136	0.036

A comparison of these results gives clear advantages for the benefit of using target information, because the geometry to calculate the corners by means of the image gradients is poor in some cases. Therefore optimization strategies to fix the camera positions are recommended. The

estimation of the accuracy of image coordinates a posteriori amounts to  $\hat{\sigma}_0 = 5.5 \times 10^{-4}$  (cm) and corresponds to about 20% of the pixel size.

## 5. Conclusions

The aim of the paper is to show up the potential of digital close range photogrammetry. Different strategies can be used to realize an automated data flow, especially for the reconstruction of simple objects; a task often to solve in robotics and machine vision.

First experience has been given using linear operators for data pre-processing, heuristic procedures for image matching, FREEMAN chains for line following and extended bundle block adjustment for object reconstruction. The algorithms developed are robust and very fast; they will be tested in further applications.

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