# CONCEPT AND TESTING OF AN AUTOMATIC SYSTEM FOR AERIAL TRIANGULATION 

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#### Abstract

This paper presents the latest release of the system TRIADIGIT for Automatic Aerotriangulation jointly developed at the Politecnico di Milano and at the University of Parma. The system is made up of three main modules: automatic location, measurement and identification of fiducial marks (inner orientation); automatic tie point extraction; assisted ground control point measurement. Here the second module is analyzed in detail, describing the procedure for tie point selection and transfer, for improving the number of multi-ray points and for outlier rejection. Results of a series of experimental tests are reported, showing the performances of the system in dealing with block featuring different scale, image content, topography and texture.


## 1 INTRODUCTION

Automation of the Aerial Triangulation has been a hot research topic in the ninenties, in the scientific community as well as among photogrammetric companies. Several tests have been organized to compare the performances of different strategies and to highlight advantages and disadvantages of the new concept with respect to Analytical Aerial Triangulation. The announcement of one of such tests, jointly organized by ISPRS and OEEPE in 1997 (Heipke and Eder, 1998), prompted our groups to join efforts in the design and implementation of an Automatic Aerial Triangulation program. The very first release of the program, named TRIADIGIT, only takes care of the selection and recognition of tie points and was completed just in time to take part into the above mentioned test (Forlani et al., 1998). Later, two new modules were implemented: ORINT, which performs the automatic interior orientation, and APPBLOCK, which allows interactive measurement of ground or additional tie points through a graphic interface.

The core of the program, i.e. the strategy for tie point extraction and transfer, has since been updated to improve either the number of multi-ray points and the point distribution within the images, both not completely satisfactory in the preceeding tests. The original approach, based on the direct search for correspondencies in a bundle block, has not been changed, but several stages have gone through a comprehensive review, leading to a more complex iteration sequence, where bundle block adjustments are performed also at the higher level of the pyramid, to improve initial values of the orientation parameters and outlier rejection.

## 2 THE TRIADIGIT SYSTEM FOR AUTOMATIC AERIAL TRIANGULATION

### 2.1 System overview

Automatic Aerotriangulation is a complex task, involving different basic procedures. The existing systems for AAT are structured in modules, each of them performing a single stage, and TRIADIGIT is not exception. Its main components, which execute the fundamental tasks (interior orientation, tie point extraction, interactive measurement of GCPs, and bundle adjustment) may exist as stand-alone program, allowing their use in other packages.

The automatic interior orientation of every image of the block, a pre-requisite of every metric operation on the imagery, is performed first. Then follows the measurement of a minimum set of the available GCPs, carried out interactively by the module APPBLOCK, to define the photogrammetric block datum, which is needed throughout the tie point
extraction stage and to compute intermediate bundle adjustments. The last preparation stage is the image pyramids generation.

Tie points are selected and matched in a hierarchical procedure from-coarse-to-fine. At the end of each level, a robust procedure to discard gross errors is carried out, followed by a bundle adjustment to reject those outliers which have still survived and to update the EO of the block. Here a check of the results by the user is required, because if the geometry of tie/ground control points is weak, the solution may be not stable, causing the subsequent failure of the whole AAT. After this stage, the remaining GCPs can be quickly measured, because the improved EO of the block is exploited to assist the user in their localization. A final bundle adjustment ends the AAT.

### 2.2 Strategy for tie point extraction

Tie point selection, measurement and transfer within a photogrammetric block is based on some a priori information, namely a rough EO and a ground model. Apart from blocks in the mountains, where a DTM is strictly necessary, a horizontal plane and the maximum height difference in the area is enough elsewhere. The strategy for tie point transfer is based on a multi-resolution approach, starting from a pixel size of about 0.8 mm and using all the levels of the image pyramids.

The workflow is made up of three main stages:

1. improvement of the approximate exterior orientation of the block;
2. tie point densification;
3. improvement of tie point accuracy and of the number of multi-ray points.

The first stage can be skipped if a set of accurate values for the EO parameters is available (e.g. if GPS has been used during the flight). In this case the procedure may start from stage 2.
2.2.1 Preliminary data setup. The dream of an AAT program only requiring to supply the images into the storage unit, to push a button, to have lunch and then to enjoy the results of aerotriangulation is still utopian. Data preparation is required also by the best commercial packages and the knowledge of some a priori information about the photogrammetric block (number of images, pixel size), the interior orientation elements and yhe camera calibration data, is necessary. A number of processing parameters must be fixed (number of image pyramid levels, l.s. matching parameters, etc.).

The search for homologous points is directly performed on the whole block, using a bundle approach. Since the collinearity model is used in point transfer, initial values of the EO elements are required; their accuracy defines the extent of the search area.

A ground model must also be given, although a simple horizontal plane is enough for most blocks. In this case the mean height in the block area has to be provided as well as the maximum height difference.
2.2.2 Improvement of the approximate exterior orientation. This stage is carried out at the top of the image pyramids, in one or may be two levels, depending on the resolution of the original images. As a rule of thumb, with imagery having a pixel size less than $20 \mu \mathrm{~m}$ two levels are necessary, otherwise one is enough.

A set of interest points is extracted by means of the Förstner operator on every image at the lowest resolution and is stored in a file; hereafter we will refer to these points as secondary points. A sub-set of primary points is derived from each set of secondary points. If there is no a priori knowledge about block geometry, however a case seldom happening, the primary points are selected by taking the $n_{p}$ points with the highest interest value $w$, hopefully all over the image. If on the contrary the geometry of the block is approximately known, the primary areas are selected in such a way that they do not overlap. Besides, areas where only twofold points might be found are neglected, apart from the border images. The primary points act as templates in the image matching, the secondary points as slaves.

The search for homologous points is built up on two nested loops. The external loop runs on all images of the block, which become in turn primary images. The inner loop runs on all the remaining images, which become secondary images. When an image is primary, each of its primary points defines a template. Its homologous in the secondary images are looked for in two steps.

The first one defines a search window on the secondary image by projecting the template point down to the DTM and then back onto the secondary image. Window orientation and size depend on the uncertainty of EO parameters of both images and the ground model. All secondary points falling in the search window are selected as candidates and matched one at a time by l.s. template matching. The match with the largest correlation coefficient yields the (likely) homologous point, if larger than a threshold. By this procedure, the conjugate points of each primary point are looked for on the whole block, so that multi-ray points might be found.

Hopefully, a first set of tie points has now been found. Unfortunately, as many as $30 \div 40 \%$ of them are outliers: due to wrong EO the conjugate points were searched for also in areas far from the correct position. To cope effectively with the large number of mismatchings, a robust procedure for gross error rejection is implemented. Every feasible pair of images is considered and the set of common points is checked against outliers by means of two methods: a robust relative orientation (Scaioni, 2000) or a parallax analysis; using the former or the latter depends on the number of points in the pair.

The AAT procedure is now stopped and the set of "clean" tie points is adjusted by the bundle program CALGE to further remove outliers by data snooping and to improve the initial EO parameters. The top level of the image pyramids usually gives tie points with an accuracy of about $0.25 \div 0.30$ pixels. Optionally, a DTM can be computed from the object coordinates of tie points, to reduce the search window in the next level.
2.2.3 Tie point densification. Experience tells that the number of tie points found in the first stage is not enough to get in the end a strong photogrammetric block. Transfer through all the remaining levels of the image pyramids shrinks the set of about $10 \div 20 \%$ of the total amount in each level. Therefore point densification is carried out, at level $\mathrm{n}-1$ (or $\mathrm{n}-2$ ). Thanks to the larger resolution of the images, more interest points can be extracted and, by exploiting the improved EO, true matches should be found more easily.

From an operational point of view, the procedure for point transfer is the same as in the first stage, but the goal is different. The improvement of the EO is now less important, while seeking more tie points is crucial to give stability to the block. At the end of this stage the tie points found are transferred "vertically" to the next level after the bundle adjustment. Moreover, the object coordinates of tie points are backprojected from the ground onto all the images of the block, giving raise to new secondary points, so that the number of rays per point should increase wherever possible. All the tie points found (directly and by the backprojection) are then transferred to the next level.
2.2.4 Tie point refinement and improvement of multi-rays. Two tasks are executed in the third stage: first, since tie points have been measured at a coarse resolution (some hundreds micrometers) the accuracy of their measurement must be improved; second, the number of manifold points should be increased as much as possible.

Every primary point has now assigned its corresponding tie points on the other images and these don't have to be looked for any more. Interest points extracted at the top level of the image pyramids are located on well defined features, allowing a good determinability of the geometric parameters of l.s. matching. Points transferred to the next level should keep this peculiarity, but this is not possible by direct transfer (simply multiplying the image coordinates of the point by a factor 2 ). The coordinates of each primary and secondary point are therefore redefined on the new level by applying the Förstner operator on a window centered on the points transferred directly (see Figure 1). Obviously, the measurement at current level may improve the precision, but may also fail, due to inaccurate backprojection or to the appearance of new details which cause mismatchings.


Figure 1. Example of a 6-ray tie point correctly traced along 5 level image pyramids

After the measurement stage, outlier
rejection and a new bundle adjustment are performed. The remaining points are backprojected on every image of the block and then transferred to the next level. This scheme is repeated until the level 0 of the image pyramids is reached. To save time, the adjustment and the backprojection are carried out only after the levels 4 and 2, whilst after the other levels all the points found by image matching are transferred without any further processing.

### 2.3 Interior Orientation

The reconstruction of the interior orientation of every image is carried out in automatic manner by the program ORINT (Forlani et al., 1999), which performs either the measurement and the identification of the fiducial marks. Based on a multi-resolution approach, the fiducial marks are first located by using gray value cross-correlation; their position is then refined by l.s. matching. If the marks are provided by symbols, they are automatically associated to the calibration file. Finally the computation of the transformation between pixel and image coordinate systems is carried out with a robust method.

### 2.4 Measurement of Ground Control Points

The program APPBLOCK performs the interactive measurement of GCPs with subpixel accuracy, thanks to image resampling. This solution is the best suited to natural GCPs, which are widely used in Italy. Apart from the measurement in strict sense, the program assists the user in the management of photogrammetric observation files. Windows from all images where the GCP is likely to be are displayed, based on the available exterior orientation and DTM. At the beginning of the AAT of a block, a minimum number of GCPs is measured to constrain the block during the intermediate bundle adjustments; this task is performed with only a rough information about the block orientation. After tie point extraction, other GCPs may be added, this time by using a more accurate exterior orientation.

This procedure may be applied also to the measurement of tie points in interactive aerotriangulation or to introduce additional observations in areas of the block where the automatic extraction failed.

## 3 RESULTS OF EXPERIMENTAL TESTS

### 3.1 Description of the tests

In this section some tests on the performance of the latest release of TRIADIGIT are reported. The theoretical accuracy of tie point extracted has been investigated by looking at the outcome of the bundle block adjustment and an independent check of their accuracy has been obtained by comparing the results of AAT to those of interactive aerotriangulation. Keeping into account the above-mentioned goals, only small blocks have been considered, resulting in manageable data volumes and not involving too much computation time. Operational aspects of AAT have been neglected. According to these guidelines, four blocks have been selected among those delivered on the occasion of the OEEPE-ISPRS test (Heipke and Eder, 1998) and those available at the University of Parma: they differ by scene contents, topography, cameras, scales, film material and overlap. Table 2 reports the main features of the blocks; Figure 3 shows for each block an image and a patch representative of the texture

| Project name | Lucera | Echallens | Botticino | OSU |
| :--- | :---: | :---: | :---: | :---: |
| Scene content | country, small town | open, partly forest | rock quarry | built-up, partly trees |
| Scene topography | flat, partly hilly | flat | very steep | flat, buildings |
| Average image scale | $1: 7500$ | $1: 5000$ | $1: 5600$ | $1: 4000$ |
| Camera (focal lenght, mm) | Wild RC10 (150) | Wild RC10 (150) | Zeiss RMKA (150) | Wild RC10 (150) |
| Film material | $\mathrm{B} / \mathrm{W}$ | B/W | $\mathrm{B} / \mathrm{W}$ | FIR |
| No. of images per strip | $6 \times 3$ | $3 \times 3$ | $3 \times 2$ | $3 \times 3$ |
| Overlaps | $\mathrm{l}=60 \%, \mathrm{q}=60 \%$ | $\mathrm{l}=60 \%, \mathrm{q}=30 \%$ | $\mathrm{l}=80 \%, \mathrm{q}=60 \%$ | $\mathrm{l}=60 \%, \mathrm{q}=60 \%$ |
| Pixel size $(\mu \mathbf{m})$ | 25 | 20 | 25 | 25 |
| Source | DIIAR, Milan | EPFL, Lausanne | Comune di <br> Botticino | The Ohio State <br> Univ. / TU Munich |
| No. and kind of GCPs | 8 (natural) | 44 (signalized) | 8 (natural) | not available |

Table 2. Description ot the data sets used in the tests


Figure 3. Examples of images and details of the texture from the blocks used for the tests

### 3.2 AAT setup and preprocessing

The inner orientation, computed by program ORINT, gave a mean sigma nought of the transformation from pixel to image coordinates for each block ranging from 0.2 to 0.5 [pel]. A minimum set of GCPs was measured in each block, to compute the bundle adjustments of each hierarchical level, except for block "OSU", where no GCPs are available and the adjustment has been computed by constraining 7 EO parameters.
3.2.1 Approximate exterior orientation. The blocks "Echallens" and "OSU", delivered on the occasion of the OEEPE-ISPRS test, were already provided with approximate values of the exterior orientation parameters, accurate to about 50 m for the projection centers and $2^{\circ}$ for the attitude angles. Besides, the overlaps were given as well. These values have been directly used. In the other two blocks ("Lucera" and "Botticino") every image has been roughly georeferenced on a map at the scale 1:25000, obtaining approximate values for the horizontal coordinates of the projection centres with an accuracy of about 100 m , and values for angles $\kappa$ with an accuracy of about $3^{\circ}$. For the elevation $\mathrm{Z}_{0}$ the instrumental flight heights registered on each photograph have been used (accuracy about 50 m ), while the angles $\omega$ and $\phi$ have been put equal to zero. This demonstrates that the derivation of the approximate exterior parameters without GPS on board is not critical, because the procedure converged despite the low accuracy .
3.2.2 Ground model. For all the blocks a horizontal plane has been adopted as ground model. For blocks "Lucera" and "Botticino" the average height and the maximum variation in elevation have been derived from an existing map. For blocks "Echallens" and "OSU", the average height of the ground was given, while the variation has been guessed according to the kind of topography.
3.2.3 Program control parameters. We tried to find standard values for the control parameters, independent of the block characteristics: e.g. we found that a 6 levels image pyramid may be used with image resolutions in the range $20 \div 30 \mu \mathrm{~m}$. Another critical point is the size of the window for l.s. matching: after many trials, we concluded that the best results may be obtained by increasing by two pixels the size of the window at each level of the image pyramid, starting from a size of 9 pixels.
3.2.4 AAT strategy. By AAT strategy we mean the setup of tie point extraction workflow, i.e. the number of image pyramid levels involved in the refinement of initial EO parameters (see par. 2.2.2), how many times intermediate bundle adjustments are computed and the backprojection of tie points is performed to increase multi-ray points. For all the blocks we followed this strategy, except for "Botticino":

1. improvement of approximate EO involving only the initial level (level 5) of the image pyramids;
2. tie point densification at level 4: after the bundle adjustment, all the tie points found are backprojected from the ground to the images;
3. in the remaining levels (3-0), tie points are traced along the image pyramids; an intermediate bundle adjustment followed by the backprojection of tie points is executed after level 2 ;
4. after level 0 the final bundle adjustment is computed.

This solution still recovers many multi-ray points which have been lost, avoiding to compute the bundle adjustment at the end of each level.

In case of block "Botticino", flown over a hilly area, a DTM has been computed at the end of the initial level by all the tie points found and used in the next level for tie point densification. In case of complex topography, where the availability of a rough DTM would facilitate tie point transfer, the test on block "Botticino" has shown that also the ground model defined by the tie points represent an effective solution.

### 3.3 AAT outcomes

3.3.1 Tie point distribution. The geometric distribution of tie points over the block and the amount of manifold points is the key for an accurate and stable aerotriangulation. Table 4 reports the number of tie points found and that of multiray points. For the blocks "Lucera", "Echallens" and "OSU" a consistent set of points has been found, as you can see in Figure 6; only multi-ray points have been drawn. The best results have been gained in case of block "Echallens", where the flat terrain and the well-contrasted image texture represent an ideal condition for AAT. On the contrary, a smaller set of tie points has been found for block "Botticino", which features many critical conditions, such as a complex topography with many breaklines, woods, areas whith poor texture.
3.3.2 Outcomes of bundle adjustment. Table 5 reports the results of the bundle adjustment in terms of sigma nought and the accuracy of tie points in object space, which are representative of the block accuracy. As far as $\sigma_{0}$ is concerned, we expected lower values, because the potential accuracy of l.s. matching is better than 0.4 [pel] and the tie point set is consistent and well distributed. The reason of this result is likely to arise from the bundle adjustment, which should use a robust method; indeed, the internal blunder detection procedure copes effectively with gross errors, but does not the same with small outliers. For the block "Echallens" the result is satifying, but also in this case it might be further improved by adopting a robust bundle adjustment.

The theoretical accuracy of object coordinates obtained of the blocks are sufficiently accurate according to image scale and terrain characteristics.
3.3.3 Independent accuracy check. Though standard deviations of tie points and external reliability may highlight weaknesses in the block, deformations cannot be traced without an external check. We therefore performed an independent test, adopting the same procedure of the OEEPE-ISPRS test (Heipke and Eder, 1998).

| Project | No. of image pyramids levels | Av. no. of rays per points | No. of multi-ray points in object space |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Total | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| Lucera | 6 | 2.7 | 2838 | 1679 | 669 | 284 | 157 | 47 | 2 | 0 | 0 |
| Echallens | 6 | 2.5 | 1607 | 1041 | 335 | 164 | 27 | 20 | - | - | - |
| Botticino | 6 | 2.5 | 306 | 173 | 103 | 25 | 5 | 0 | - | - | - |
| OSU | 6 | 2.8 | 1330 | 772 | 289 | 121 | 63 | 58 | 22 | 5 | 0 |

Table 4. Multi-ray tie points at the end of AAT

| Project | $\sigma_{0}$ of bundle adjustment |  | Ratio equations/ unknowns | No. of GCPs used | No. of check points | Theoretical accuracy [cm] |  | RMS of residuals on check points [cm] |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | [pel] | [ $\mu \mathrm{m}$ ] |  |  |  | $\sigma_{\text {X.Y }}$ | $\sigma_{\mathrm{Z}}$ | $\sigma_{\mathrm{X}-\mathrm{Y}}$ | $\sigma_{\mathrm{Z}}$ |
| Lucera | 0.50 | 12.6 | 1.75 | 8 | 106 | 8.8 | 22.8 | 8.4 | 16.1 |
| Echallens | 0.27 | 5.4 | 1.67 | 8 | 55 | 3.4 | 7.5 | 3.8 | 7.9 |
| Botticino | 0.54 | 13.4 | 1.65 | 8 | 59 | 10.1 | 30.5 | 6.2 | 13.4 |
| OSU | 0.32 | 9.6 | 1.86 | - | 60 | 5.1 | 9.2 | 8.8 | 11.3 |

Table 5. Results of bundle adjustment and residuals on check points


A set of well distributed tie points has been interactively measured by means of the program APPBLOCK in each block. The same interior orientation parameters were applied, so both sets of image coordinates ("automatic" and "manual") are homogeneous. The "manual" block has been adjusted by using the same constraints and the object coordinates of tie points have been computed. Then the image and object coordinates of tie points belonging to the "manual" block have been inserted as check points in the adjustment of the block made up by the "automatic" measurements. The discrepancies between these two data sets are reported in Table 5. The RMS computed in this way may be assumed as the accuracy of "automatic" measurements. Differences with respect to the theoretical accuracies (Table 5), are always very small, ensuring that the ties within the "automatic" block are strong enough. The larger discrepancies in height might be due also to the weakness of the "manual" blocks, which should be strenghtened by introducing more tie points.

## 4 CONCLUSIONS

In this paper we described the new features of our AAT program TRIADIGIT. The tests made show that the program is now operational, though not ready for mass production, and can cope with demanding environments. As far as the procedure is concerned, outlier rejection should be slightly modified, since too many points are rejected on the border of the block. As far as the workflow is concerned, the switch from bundle block adjustment to point transfer should be improved, ensuring a larger degree of automation. For the time being, the performance in terms of computing time is still unsatisfactory: the average time in the four block turned out to be around 6 hours on a Pentium I 200MHz: software optimization is required. A graphic user interface is also being developed, to improve the data preparation.

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