

## SEAM SMOOTHING OF DIGITAL COLOR MOSAICS

Hao-Hsiung Huang  
Associate Professor

Department of Surveying and Mapping Engineering  
Chung Cheng Institute of Technology  
Tahsi, Taoyuan, 335 Taiwan, Republic of China  
Commission IV

### ABSTRACT:

The discontinuous tone and unavoidable seam between photos due to image mismatching can usually be detected on a traditional controlled mosaic. To minimize this detectable effects and establish an efficient digital mosaic system is thus the purpose of this paper. Polynomial fitting technique has been used to define seams which are then eliminated by the use of smoothing.

The system was tested by producing two controlled mosaics from two blocks of color images respectively, taken under various photo distances and illuminations by the use of a CCD camera. These two mosaics were found to be of high compatibility.

**KEY WORDS:** Digital Mosaics, Seam Smoothing, Image Processing

### 1. INTRODUCTION

Traditionally, the discontinuous tone and unavoidable seam between photos due to image mismatching can easily be visualized when two or more images of a scene are mosaicked. The computer methods for digital mosaics would minimize the degree of mismatch (Milgram, 1975; 1977).

Most papers concerned with mosaics discussed images acquired by satellite. Very few authors have covered digital mosaics using a set of pictures taken by a CCD camera. Various factors intervene to make the mosaicking of CCD images difficult (Jensen, 1986). Cameras uncertainty and lens distortion can cause registration error.

However, digital images can be obtained quickly and cheaply by using a CCD camera. It is thus worth studying how to rectify CCD images and combine them together.

As described by Milgram (1977), images were registered respectively firstly, gray-levels of two adjacent images were then equalized, and seam was defined and smoothed finally. In this paper, the author uses similar procedures and additionally presents a simple method that makes tone vary continuously from one image to the next. Seam is also defined as a polynomial curve, and so smoothed that the final mosaic looks like a single image.

### 2. RECTIFICATION

Resampling technology is used to rectify the deformed images. Any of three resampling methods, nearest neighbor, bilinear interpolation, and bicubic interpolation can usually be adopted (Lillesand and Kiefer, 1987). Since bicubic interpolation gives the best image quality, it has therefore been used throughout in this study.

Three rectification methods, polynomial rectification, projective transformation, and differential rectification are commonly used in image processing systems (Novak, 1992). Two-dimensional projective transformation equations can complete the analytical rectification of a tilted image (Wolf, 1983). Since a CCD camera as used in this study, usually

takes a tilted image. Equations as shown below, of a two-dimensional projective transformation were thus applied for rectification.

$$\begin{aligned} X &= \frac{a_1 x + b_1 y + c_1}{a_3 x + b_3 y + 1} \\ Y &= \frac{a_2 x + b_2 y + c_2}{a_3 x + b_3 y + 1} \end{aligned} \quad (1)$$

Where

$a_1, a_2, a_3, b_1, b_2, b_3, c_1, c_2$  are the transformation parameters,  
 $X, Y$  are coordinates of the original image, and  
 $x, y$  are coordinates of the registered image.

More than four control points are required to obtain a least squares solution for the parameters in Eqs. (1).

### 3. TONE CONTINUOUS

Let L be the left image and R be the right image. These two images have been registered respectively and have to be mosaicked. Two histograms of their respective overlap areas,  $Q_l$  and  $Q_r$  would be ideally identical. But various illuminative conditions affect the histograms differentially. Hord (1982) mentioned that the gray-levels of the two images could be so stretched that the average gray-levels,  $\mu_l$  of  $Q_l$  matched the average gray-levels,  $\mu_r$  of  $Q_r$ .

Let  $\sigma_l$  and  $\sigma_r$  be the standard deviations of gray-levels of  $Q_l$  and  $Q_r$  respectively. When the L and the R images were been processing, the following equations could be used to improve the Hord's method.

$$\begin{aligned} G_l' &= \frac{G_l - \mu_l}{\sigma_l} \sigma + \mu \\ G_r' &= \frac{G_r - \mu_r}{\sigma_r} \sigma + \mu \end{aligned} \quad (2)$$

Where

$$\begin{aligned} \mu &= (\mu_l + \mu_r)/2 \\ \sigma &= (\sigma_l + \sigma_r)/2 \end{aligned} \quad (3)$$

$G_l$  and  $G_r$  are the input gray-levels of the left and right images respectively, and  $G_l'$  and  $G_r'$  are the output gray-levels of the left and right images respectively.

Owing to light falloff problem, global adjustment method as just described, will not eliminate significant artificial edges. One can expect that this degree of appearance can be decreased by processing on a row by row basis. Let  $\Delta_1, \Delta_2, \dots, \Delta_n$ , be the differences of average gray-levels for each row in  $Q_l$  and  $Q_r$ . Here,

$$\Delta_i = \sum_{j=1}^n (L_{ij} - R_{ij})/n \quad (4)$$

$Q_l$  and  $Q_r$  have the same sizes of  $m$  rows by  $n$  columns. In general, the  $\Delta$ 's could be assumed vary continuously from one row to the next. Therefore, they would be fitted using a polynomial transformation equation as expressed below.

$$\Delta_i = a_0 + a_1 i + a_2 i^2 + a_3 i^3 + \dots \quad (5)$$

When equations of the type of Eq.(5) have been written for all rows, a least squares solution can be obtained for the parameters in Eq.(5). These parameters are then used in Eq.(5) to compute the regressive values of the  $\Delta$ 's for each row.

The new  $\Delta_i/2$  values are then subtracted to each pixel of the corresponding row on the left image, and added to each pixel of the corresponding row on the right images. The resultant images can be prepared for the "seam definition and smoothing" step as described below.

#### 4. SEAM DEFINITION AND SMOOTHING

As stated by Milgram and Hord, a seam point for each row can be defined by the following equation.

$$D_j = \sum_{k=-w/2+1}^{w/2} |L_{j+k} - R_{j+k}| \quad (6)$$

Where  $D_j$  are the sums of differences over  $w$  pixels, and  $j$  would be found when  $D_j$  is minimal. The seam point would then be located at pixel  $j$  on the current row.

However, horizontal positions of a succession of seam points obtained by this method are unrelated to each other. This usually causes horizontal artificial edges on the mosaics. In avoiding this appearance, one can restrict that the seam points positions,  $j$  vary continuously from one row to the next. Again, a polynomial transformation equation similar to Eq.(5) would be applied, and  $j$  is substituted for  $\Delta$ , as follows:

$$j_i = a_0 + a_1 i + a_2 i^2 + a_3 i^3 + \dots \quad (7)$$

A type of Eq.(7) can be written for each row, and  $m$  equations may be formed containing the four unknown parameters. The equations are solved by the method of least squares to obtain the most probable transformation parameters. These parameters are then used in Eq.(7) to compute the adjusted values of the  $j$ 's for each row.

Once a seam point has been determined, the image information in the mosaic to the left of the seam point will come from the line segment of image  $L$ , and the information to the right from the the image  $R$ . Fig.1 shows gray-levels of sample overlapping windows.

The smoothing of the gray-levels changed at each of the seam points is the final step. A ramp function expressed by Milgram (1975) may be adopted.

#### 5. EXPERIMENT

A colorful original was chosen in this study. Thirty grided targets were marked on the original, and were used for control points. Two blocks of color images respectively, using red, green, and blue filters individually, were taken under various photo distances and illuminations by the use of a CCD camera. One block was composed of two pictures as shown in Fig.2, and the other one was composed of three pictures as shown in Fig.3.

Image coordinates of control points on each of five pictures were then measured. These coordinates ( $X, Y$ ) and their corresponding theoretical coordinates ( $x, y$ ) on the rectified images were used to compute the transformation parameters. Each of the original images was then registered by the use of these parameters and resampling technology.

Two controlled mosaics were then produced respectively, using the process indicated previously. The first mosaic shown in Fig.4, was generated from two registered images. The second one shown in Fig.5, was generated from three registered images. The difference of two mosaics was processed and shown in Fig.6. The two mosaics are found to be of high compatibility. A seam curve is also visible in Fig.6.

#### 6. CONCLUSIONS

Based upon the results of this study, several conclusions can be drawn, as follows:

- (1) The accuracy of geometric registration strongly influences the quality of a mosaic. In order to successfully mosaic the adjacent images, the method of the geometric transformations must be considered. A two-dimensional projective transformation used in this study is good enough for registration of the images on two non-parallel planes.
- (2) Tone continuous processing of the adjacent images results in enhancing the effect of a smooth transition across the seam. The seam points positions can thus vary continuously, as expected, from one row to the next.
- (3) Cameras uncertainty and lens distortion may introduce geometric errors of an image. Investigation on eliminating these errors should be considered.
- (4) The polynomial fitting model was used in two aspects, tone change and seam points change from one row to the next. Further study of using another model would be desirable.

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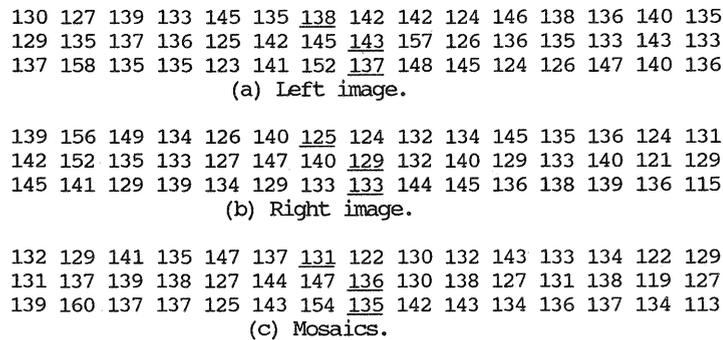


Figure 1. Gray-levels of sample overlapping windows. The underlined values locate seam points.

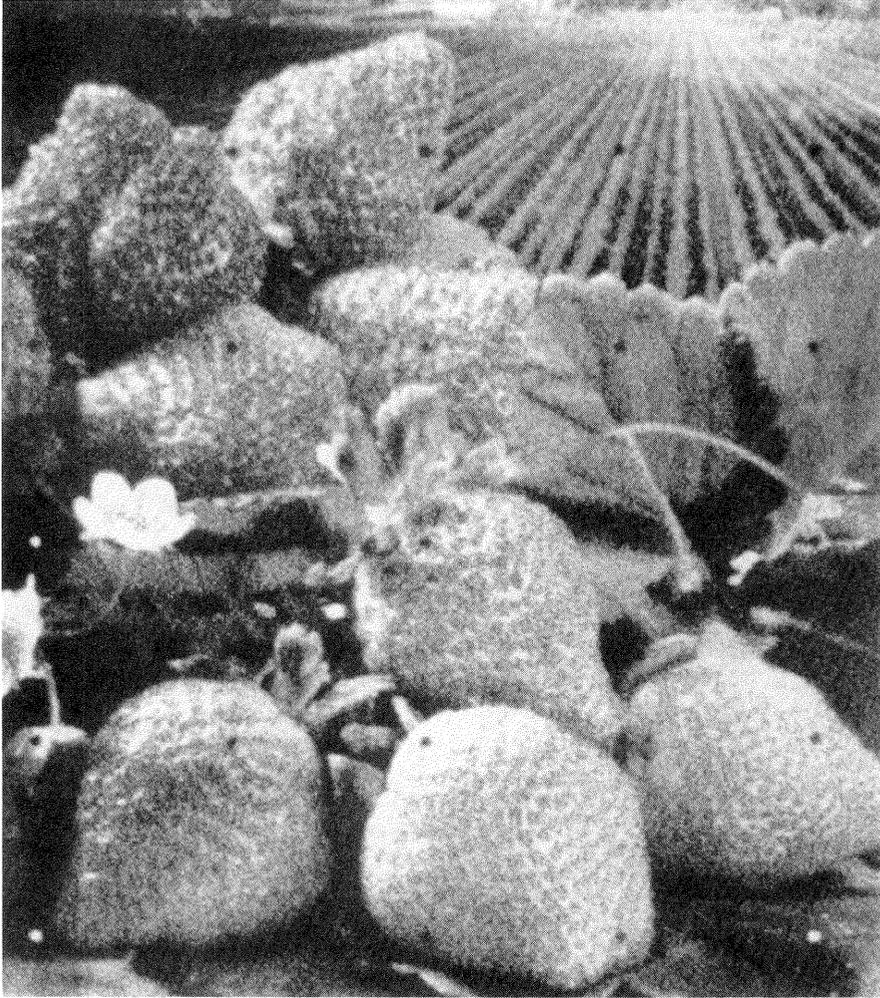


Figure 2. Two registered images. Seam is visible.

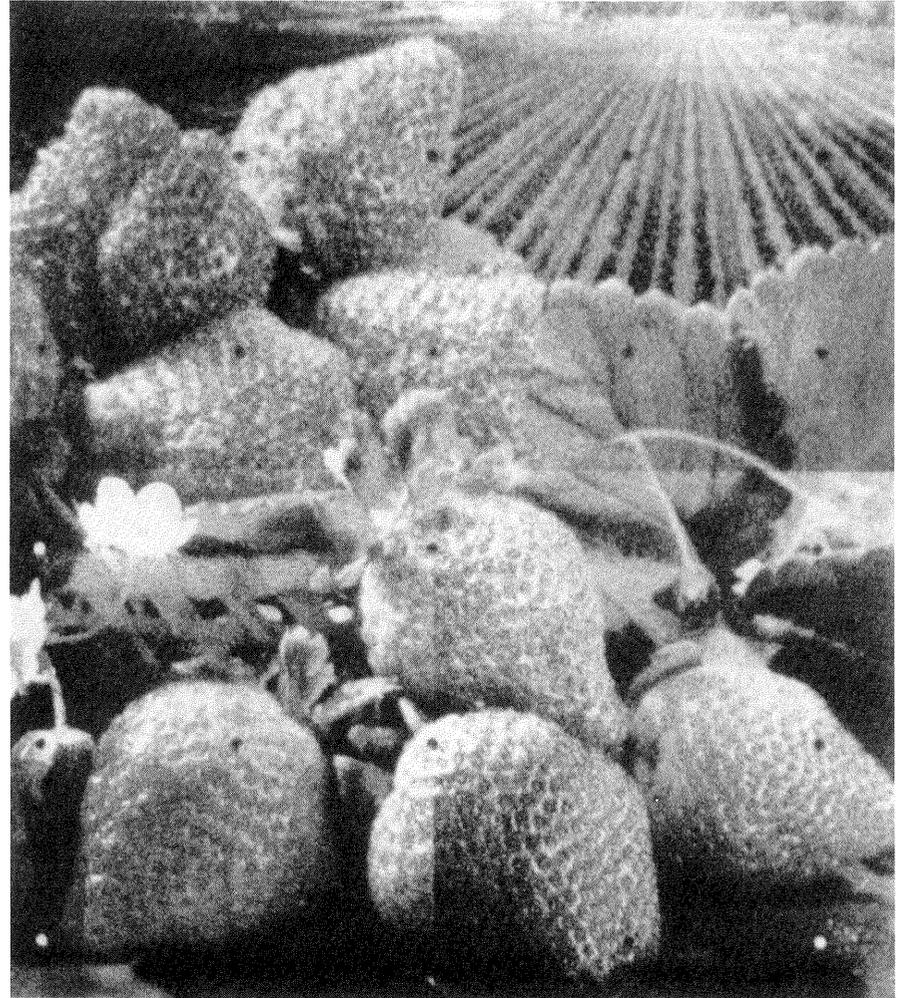


Figure 3. Three registered images. Seam is visible.

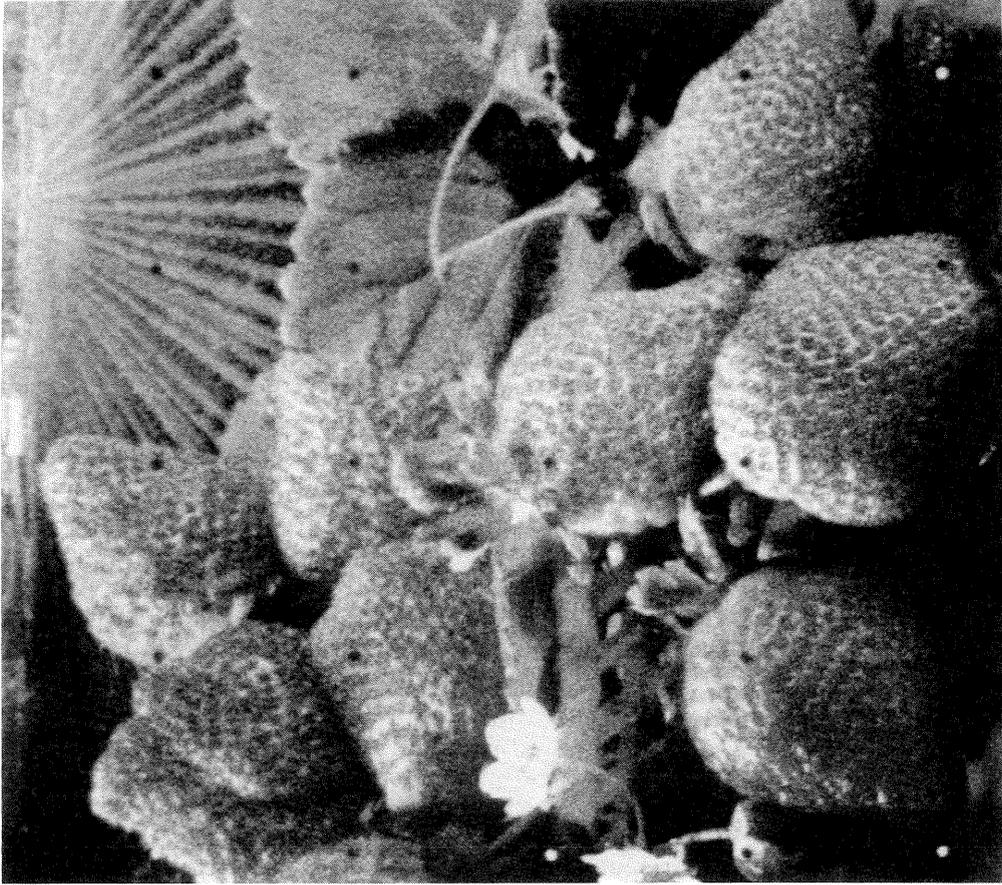


Figure 5. Mosaic of Fig.3.

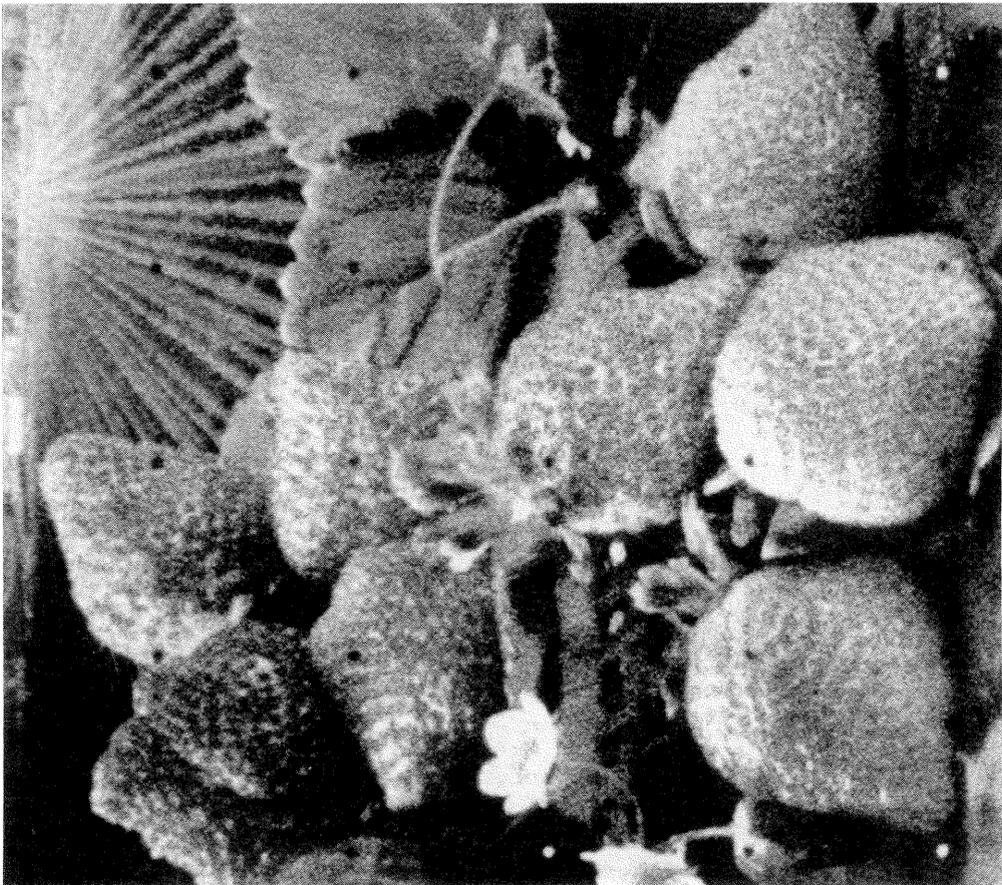


Figure 4. Mosaic of Fig.2.

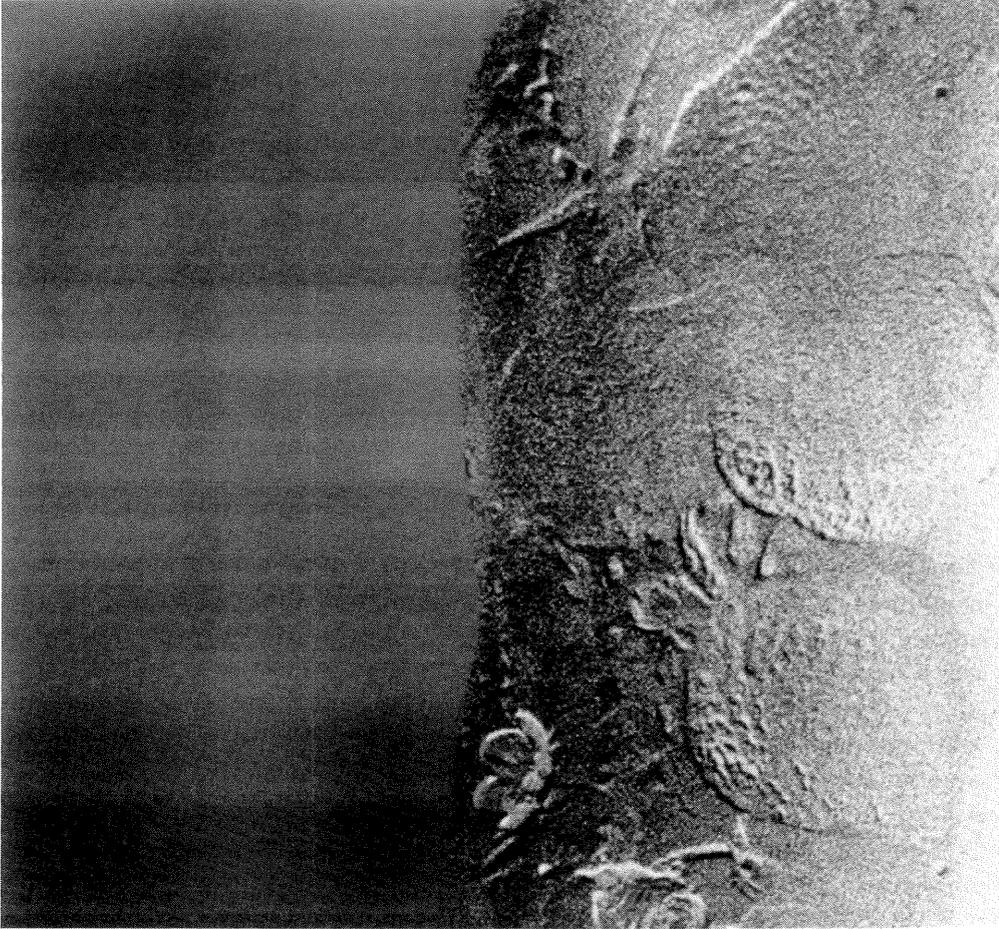


Figure 6. Difference of Figs. 4 and 5, with seam curve made visible.