DATA FUSION AND VISUALIZATION OF PANORAMIC IMAGES AND LASER SCANS

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ABSTRACT

The paper describes the use of a laser range finder and a rotating CCD line camera for scanning and visualizing panoramic (360°) indoor scenes. The paper describes coordinate systems of both sensors, specifies the fusion of depth and texture data acquired by both sensors, and reports on three different alternatives for visualizing the generated 3D data set. Compared to earlier publications the recent approach also utilizes an improved method for calculating the spatial (geometric) correspondence between laser diode of the laser range finder and the focal point of the rotating CCD line camera. Calibration is not a subject in this paper; we assume that calibrated parameters are available utilizing a method as described in (R. Reulke and Scheibe., 2003).

1 INTRODUCTION

Laser range finders (LRFs) have been used for close-range photogrammetry (e.g. acquisition of building geometries) for several years, see (Niemeier., 1995, Wiedemann., 2001). A LRF which is based on the frequency to distance converter technique has a sub-millimeter accuracy for sensor-to-surface distances which are between less than one meter and about 15 meters. In earlier publications (F. Huang and Scheibe., 2002) we demonstrated how to fuse LRF data with pictures (i.e., colored surface texture) obtained by a rotating CCD line sensor (which we call the camera in this paper). Both devices are independent systems and can be used separately. To be precise, three CCD lines (red, green and blue channel) capture a color picture, and the length of these lines is in the order of ten thousand cells (pixels), producing pictures of several gigabytes during a 360° scan.

The fusion of range data and pictures for 3D scene rendering is a relatively new development; see e.g. (Kern., 2001) for combining range data with images acquired by a video camera. Combinations of panoramic images (Benosman and Kang, 2001) and LRF data provide a new technology for high-resolution 3D documentation and visualization. Fusion of range data and panoramic images acquired by a rotating line camera has been discussed in (F. Huang and Scheibe., 2002, R. Klette and Reulke, 2003). Calibration of range sensors (F. Huang and Scheibe., 2002) and of rotating line cameras (F. Huang and Klette., 2002) provide necessary parameters for this process of data fusion. In this paper we assume that parameters have been calibrated, and we do not elaborate on calibration details, but provide a brief indication of related calibration needs.

The main subject of this paper is a specification of coordinate transformations for data fusion, and a discussion of possible ways of visualizations (data projections).

The approach in (F. Huang and Scheibe., 2002) combines several LRF data sets with several camera data sets by mapping all data into ortho planes. This simplified approach (known from processing of orthophotos) utilizes a 2.5 D surface model for the LRF data, and no complex ray tracing or volume rendering is needed. This simplified approach assumes the absence of occluding objects between LRF or camera, and ortho surface. In a first step we determine the viewing direction of each pixel of the camera (described by a formalised sensor model) towards the 2.5 D surface sampled by the LRF data. This can be done if both devices are calibrated (e.g., orientations of the systems in 3D space are known in relation to one world coordinate system) with sufficient accuracy. Requirements for accuracy are defined by the desired resolution in 3D scene space. Orientations (i.e., affine transforms) can be specified using control points and standard photogrammetry software. The 2.5 D model of ortho-surfaces is generated by using several LRF scans to reduce the influence of shadows. More than a single camera viewpoint can be used for improved coloration (i.e., mapping of surface texture). Results can be mapped into several ortho planes, which can be transformed into a unified 3D model in a second step. See Figure 1.

In this paper we discuss a more advanced approach. For coloration of an extensive 3D point cloud, generated from several LRF data sets, we use captured panoramic images obtained from several camera scans. This requires an im-

Figure 1: A (simple) 3D CAD model consisting of two ortho planes.
plementation of a complex and efficient raytracing algorithm for an extremely large data set. Note that this raytracing cannot assume ideal correspondences between points defined by LRF data and captured surface texture; we have to allow assignments within local neighborhoods for identifying correspondences between range data and surface texture. Figure 2 illustrates this problem of local uncertainties.

![Figure 2: Raytracing problem when combining one LRF scan with data from one camera viewpoint.](image)

There are different options to overcome this problem. A single LRF scan is not sufficient to generate a depth map for a complex 3D scene. Instead of fusing a single LRF scan with color information, followed by merging all these fused scans into a single 3D model, we prefer that all LRF scans are merged first into one unified depth representation of the 3D scene, and then all camera data are used for coloration of this unified depth representation. Of course, this increases the size of data sets extremely, due to the high resolution of LRF and camera. For simplification of raytracing, the generated 3D points can be first used to create object surfaces by triangulation, applying standard routines of computer graphics. This can then be followed by raytracing, where the parametrization obtained in triangulation (including routines for simplification) reduces the size of the involved sets of data.

LRF and camera will have different viewpoints or positions in 3D space, even when we attempt to have both at about the same physical location. A simple approach for data fusion could be as follows: for a ray of the camera map the same physical location. A simple approach for data fusion is to allow assignments within local neighborhoods for identifying correspondences between range data and surface texture. Figure 2 illustrates this problem of local uncertainties.

No ray tracing algorithm is necessary for this step because occlusions do not need to be considered. The result is a colored 3D point cloud. Nevertheless, to model the data it is necessary to triangulate the LRF points into a mesh (because LRF rays and camera rays do not ideally coincide). A triangulation reduces the number of points and makes it possible to texture the mesh. Note that using this approach the same shadow problem can occur as briefly discussed above for single LRF scans.

This more advanced approach requires to transform the panoramic camera data into the LRF coordinate system. In order to cover the 3D scene completely, several scans are actually required from different viewpoints, which need to be merged to create a 3D mesh (also called wireframe). Points obtained from one LRF scan are connected with points obtained from another LRF scan. In this case the advantage of unique ray-to-ray assignments (assuming aligned positions and directions of LRF and camera) is lost. It is again necessary to texture a 3D wireframe by data obtained from different camera viewpoints (i.e., a raytracing routine is again required). We describe a time-efficient raytracing approach for such a static texturing situation in this paper. We report about advantages of applying independent LRF and camera devices, and illustrate by examples (e.g., results of the “Neuschwanstein project”).

The Neuschwanstein project is directed on a complete 3D photogrammetric documentation of this Bavarian castle. Figures in this paper show the Thronsaaal of this castle as scanned from the viewpoint (i.e., LRF and camera in about the same location) about at the center of the room. Of course, a more complete photogrammetric documentation used more viewpoints to reduce the impact of “shadowed areas”. The paper describes all transformations and algorithms applied in this process.

2 COORDINATE SYSTEMS

LRF and camera scans are in different independent coordinate systems. To fuse both systems it is necessary to transform the data into one primary reference system, called the world coordinate system.

Rays of the panoramic camera are defined by image rows \( i \) (i.e., this is the horizontal coordinate) and pixel position \( j \) in the CCD line (i.e., this is the vertical coordinate). Similarly, we identify rays of the LRF by an index \( i \) and a constant angular increment \( \varphi_0 \) which defines the absolute horizontal rotation angle \( \varphi = i \cdot \varphi_0 \), and an index \( j \) and an angle increment \( \vartheta_0 \) which defines the absolute vertical angle \( \vartheta = j \cdot \vartheta_0 \). Note that these absolute angles are also the same for the panoramic camera. However, the possible range of vertical angles of the camera is typically reduced compared to that of a LRF; the possible range of horizontal angles of the LRF is typically reduced compared to that of a panoramic camera.

2.1 LRF

A LRF scans in two dimensions, vertically by a deflecting mirror and horizontally by rotating the whole measuring
system. The vertical scan range is 310° (which leaves 50° uncovered), and the horizontal scan range is 180°. The LRF scans overhead, therefore a whole sphere will be scanned with one 180° moving. Fig. 3 depicts a LRF raw data set and the not calibrated image.

Figure 3: Raw data of the not calibrated LRF image.

Rays and detected surface points on these rays (which define the LRF data set) can be described in a polar coordinate system. According to our application of the LRF, it makes sense to transform all LRF data at one viewpoint into a normal polar coordinate system with a horizontal range of 360° and a vertical range of 180° only. At this step all LRF calibration data are available and required.

The photogrammetry specify for rotating measuring devices, e.g. theodolite systems, how to measure the errors along the rotating axis. They called vertical and horizontal collimation errors. The pole columns describe the column around the zenith, the highest point in the image. To determine the collimation errors, typically the to measured point will be located by two sites. That means the point will be measured in two steps, first measured in site one, than the rotation axis will turn by 180° and the point will be measured again (Däumlich and Steiger, 2002). Fig. 4 depicts the optical Z-axis and an orthogonal K-axis. A range finder measures along a variable Z-axis, which may be effected by horizontal (i.e., along the Z-axis) or vertical (i.e., along the K-axis) errors.

The horizontal and vertical collimation errors are calculated by determining the pole column (this can be done in the LRF image based on two rows [layers] and identical points at the horizon). This provides the offset to the zenith and to the equator (i.e., the horizon). The horizontal collimation error can be calculated by control points along the equator. The vertical collimation error can be determined based on these results. As an important test we have to confirm that the zenith is uniquely defined in 3D space for the whole combined scan of 360°.

Each point in the LRF coordinate system is described in polar or Cartesian coordinates as a vector \( \mathbf{p} \), which is defined as follows:

\[
\begin{align*}
p_x &= R \cdot \sin \vartheta \cdot \cos \varphi \\
p_y &= R \cdot \sin \vartheta \cdot \sin \varphi \\
p_z &= R \cdot \cos \vartheta
\end{align*}
\]

The orientation and position with respect to a reference vector \( \mathbf{p} \) in the world coordinate system is defined by one rotation matrix \( \mathbf{A} \) and a translation vector \( \mathbf{r}_0 \):

\[
\mathbf{p} = \mathbf{r}_0 + \mathbf{A} \cdot \mathbf{p}
\]

All coordinate systems are right hand systems. The laser scanner rotates clockwise. The first scan line starts at the positive y-axis in the LRF system at the horizontal angle of 100 gon\(^1\). The rotation matrix combines three rotations around all three axes for the right hand system:

\[
\begin{align*}
\mathbf{A} &= \mathbf{A}_\omega \cdot \mathbf{A}_\phi \cdot \mathbf{A}_\kappa
\end{align*}
\]

The resulting matrix \( \mathbf{A} \) is then given as

\[
\begin{pmatrix}
C_\omega & S_\omega & 0 \\
-S_\omega \cdot C_\kappa + C_\omega \cdot S_\phi & S_\omega \cdot S_\kappa + C_\omega \cdot C_\phi & S_\phi \cdot S_\kappa \\
S_\omega \cdot S_\kappa + C_\omega \cdot C_\kappa & -S_\omega \cdot C_\phi + C_\omega \cdot S_\kappa & C_\phi \cdot C_\kappa
\end{pmatrix}
\]

where \( \kappa, \phi, \omega \) are the rotation angles around the z-, y-, and x-axis, respectively, and \( C \) stands short for the cosine and \( S \) for the sine.

\(^1\)The unit gon is defined by 360° = 400 gon.
2.2 Camera

The panoramic image sensor is basically a rotating CCD line sensor. Three CCD lines are mounted vertically and also rotate clockwise. The scanned data are stored in cylindrical coordinates. In an ideal focal plane each pixel of the combined (i.e., all three color channels) line is defined by the vector $\vec{r}_d$. The rotation axis of the camera is incident with the main point of the optics. The focal plane is located at focal length $f$, without any offset $\Delta$. Scans begin at the horizontal angle of 100gon. We have the following:

$$\vec{r}_d = \begin{pmatrix} r_{dx} \\ r_{dy} \\ r_{dz} \end{pmatrix} = \begin{pmatrix} 0 \\ f \\ j \cdot \delta \end{pmatrix}$$

(3)

The used CCD line had a length of approximately 70mm and it had 10,296 pixels with a pixel size $\delta = 7\mu m$ indexed by $j$. Each scanned surface point is identified by the camera rotation $A_\varphi$. In analogy to the LRF, a reference vector (in world coordinates) for the camera coordinate system is described by the rotation matrix $A$ as follows:

$$\vec{r} = \vec{r}_0 + A \cdot \lambda \cdot A_\varphi \cdot \vec{r}_d$$

(4)

$\lambda$ is an unknown scale factor of the camera coordinate system (for the 3D scene). If the LRF and the camera systems have the same origin, then $\lambda$ corresponds to the distance measured by the laser scanner. We also model the following deviations from an ideal case:

- The CCD line is tilted by three angles regarding the main point ($A_I$).
- The CCD line has an offset vector regarding the main point ($\Delta$).
- The optical axis is rotated regarding the rotation axis ($A_O$).

These deviations are depicted in Figure 6 and described in the following equation:

$$\vec{r} = \vec{r}_0 + \lambda \cdot A_\varphi A_O \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} \Delta_x \\ \Delta_y \\ \Delta_z \end{pmatrix}$$

(5)

For the calculation of calibration parameters $A_{opt}$, $A_{in}$ and the offset $\Delta$, see (F. Huang and Scheibe., 2002).

3 FUSION

Fusion of the data sets starts with transforming both coordinate systems (i.e., LRF and camera coordinate systems) into one world coordinate system. For this step the orientation of both system needs to be known. A transformation of LRF data into the world coordinate system is then simple because all required parameters of the equation are given. It is only necessary to determine the orientation to the world coordinate system as shown in Equation 1. For the camera data the parameter $\lambda$ is unknown, which can be estimated by Equations 1 and 5. By applying all parameters of the interior and external orientations to the vector $\vec{r}_d$ the following simplified equation results:

$$\vec{r} = \vec{r}_0 + \lambda \cdot \vec{r}_d$$

(6)

and therefore

$$\begin{pmatrix} r_x - r_{0x} \\ r_y - r_{0y} \\ r_z - r_{0z} \end{pmatrix} = \begin{pmatrix} r_{dx} \\ r_{dy} \\ r_{dz} \end{pmatrix}$$

(7)

and $\lambda$ e.g.

$$\lambda = \frac{r_y - r_{0y}}{r_{dy}}$$

(8)

But the ray between a pixel and a 3D point in the LRF data set can be disturbed by an object, and a raytracing routine has to check whether the LRF point can be colored properly.

We applied an LRF and camera setup which allows to center both main points in such a way that we are able to map any LRF point or camera ray into the world coordinate system. Equations (1) and (5) reduced by the term $\vec{r}_0 + A$ are described in the following equation:

$$\vec{r} = \lambda A_\varphi A_O \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} \Delta_x \\ \Delta_y \\ \Delta_z \end{pmatrix}$$

(9)

By applying all parameters of the interior orientations to the vector $\vec{r}_d$ the following simplified equation results. $\vec{r}_d$
now describes the viewing direction of each pixel like in an ideal focal plane as shown in Equation (4), and we obtain the following:

\[
\vec{p} = \lambda \cdot A_{\varphi} \cdot \vec{r}_{d}
\]  

(10)

Note that \(\lambda\) corresponds to the distance \(R\) of the LRF to the scanned point. \(A_{\varphi}\) contains the rotation angle \(\varphi\) and represents an image column \(i\). The transformed vector represents the image row \(j\) and the number of the pixel in the CCD line. Therefore each point in the LRF coordinate system has an assigned pixel value in the panoramic image. Figure 7 depicts a flipped open sphere. Horizontal coordinates represent angle \(\varphi\) and vertical coordinates the angle \(\vartheta\) of the LRF coordinate system.

Figure 7: Panoramic image data have been fused in a sub-window of the shown range image. (The figure shows the Thronsaal of castle Neuschwanstein.)

4 VISUALIZATION

4.1 Projection

All projections are implemented with OpenGL. Generally, OpenGL is an interface which stores all transformations in different types of matrixes. All other important information can be saved in arrays (e.g., object coordinates, normal vectors and texture coordinates). The rendering engine multiplies all matrices to a transformation matrix and transforms each object coordinate by multiplying the current transformation matrix with the vector of the object coordinate. Different kinds of matrixes can be stored in stacks to manipulate different objects by different matrixes. The main transformation matrix \(M_T\) is give as follows:

\[
M_T = M_V \cdot M_N \cdot M_P \cdot M_M
\]  

(11)

\(M_V\) is the view port matrix, which is the transformation to the final window coordinates. \(M_N\) is the normalization matrix of the device coordinates, \(M_P\) the projection matrix and \(M_M\) the matrix to transform model coordinates (e.g., a rotation, scaling, or translation). All matrixes in OpenGL can be set comfortably by functions. The figure 8 depict a 3D model rendered central perceptively based on image data of Fig. 7. In this case the colored information are ignored.

In the mostly case high resolution ortho photos as final product stored in an common file format independent from the resolution of the viewport of OpenGL are necessary. The first step is to determine the attitude parameter of the

**orthogonal plane. This can be done in the 3D model. A correction of the attitude can included in this step. This means that in the most cases a ceiling or a panel, the xy-plane, or a wall, the xz-plane, is parallel to the corresponding plane in the world coordinate system. The Eq. 1 expand by the parameter \(A_{ortho}\) the attitude of the ortho plane and a factor for the resolution \(t\) is shown in the following Eq. 12. In this case are both systems are already fused to on common image. The “3D” coordinates with the appendant color information are established.

\[
\vec{o} = t \cdot A_{ortho} \cdot (\vec{r}_0 + A \cdot \vec{p})
\]  

(12)

\(o_x\) and \(o_z\) is the position in the ortho plane. If is necessary \(o_y\) can saved as the altitude in the ortho surface. The digital surface model (DSM) can be used to generate ortho photos from independent cameras or if necessary to scan without the mechanical fixes, described in the Introduction. The Fig. 9 depict the dependencies.

Figure 9: A defined ortho plane ‘behind’ the generated 3D data.
The model view can be modified by changing the matrix $M_V$, so that the 3D object can rotate or translate in any direction. The camera viewpoint can also be modified. It is possible to go into the 3D scene and look around. Further more it is possible to render more than one viewpoint in the same rendering context and create anaglyph stereo pairs by this way. The correct way to create stereo pairs is the "non symmetric frustum" method. It introduces no vertical parallax. It requires a non symmetric camera frustum, this is supported by some rendering packages, in particular, OpenGL.

Figure 10: Stereo projection of the same hall shown in Fig. 7; the anaglyph uses red for the left eye.

4.2 Triangulation

In figure 8 the measured points are shown. The high point density makes the point cloud look like a surface. But the single points become visible, when viewing a close-up of the object. An other disadvantage of this representation is that modern graphic adapters with it is 3D acceleration only support a fast rendering of triangles and triangle stripes. Polygons will tesselated\(^2\) by the graphic adapter. To render triangles it is necessary to triangulate the single points to triangles.

Because of this, the point cloud is converted in a triangle mesh. Therefore, a initial, dense mesh is generated. For the generation the incremental algorithm proposed by Bodenmueller (Bodenmueller and Hirzinger, 2004) is used. Originally, this approach is developed for online processing of unorganized data from hand-guided scanner systems. But the method is also suitable for the processing of the laser scanner data we used, because it uses a sparse, dynamic data structure which can hold larger data sets and it is able to generate a single mesh from multiple scans. The following work flow explain the principal way for the triangulation.

- tinning of points (density check)
- normal approximation (local approximation of the surface)
- point selection (insert point, depend by normal and density)
- estimation of the euclidian neighborhood relationships
- neighborhood projecting to tangent plane ( P[3D $\rightarrow$ 2D] )
- new local triangulation (Delaunay)

A second important relationship is the connectivity between the triangles. This basic relationship is important for the most algorithm for example the calculation of triangle strips, shadows or to meshing the pre triangulated points. The following section described a fast way to do this.

4.2.1 Connectivity The connectivity means, which polygon is connected by an other polygon. In the standard computer graphic and in the most cases it is not necessary to improve the algorithm to calculate the connectivity, because the most models have only a lots of polygons and it is a static pre calculation, mostly done by the initialization of the object. It is very easy to check every edge of a polygon with every all edges of all other polygons. In our case we have many millions of polygons. By implementation of the connectivity algorithm based on the Gamasutra’s article (Lee, n.d.) more than one hour was needed to calculate the connectivity. The idea is to hash the point indices to one edge index. The Fig. 11 illustrate how to hashing the edges. Every edge have two indices $n, m$. Important is by sorting the indices the first column represent the low index $n$ and the higher is $m$. Every pair $n, m$ have a uniqueness $z$. by pushing the $n$ value in the higher part of a register and $m$ in the lower part. Now we can sort the first column of our structure by $z$. Only one loop is enough to set the dependencies. If one row $i$ and row $i + 1$ have the same $z$ the dependencies are directly given by the second and third column of our structure. The row three and four in figure (Fig. 11 must have the same $z$ and the connectivity is given by column two and three: Triangle one, side three is connected by triangle two, side one. With this algorithm we need for the same scan before only 10 seconds.

4.3 Light and shading

For a better visualization and a realistic impression it is necessary to shade a scene, calculating shadows, reflections and other light features. Shading means the surface

Figure 11: Fast connectivity calculation of triangles.
shading of objects, not shadow calculations itself. Especially complex detailed structures have better depth impression, if they are shaded. Shading surfaces calculate, how much light the surface is reflecting. Three kind of light contributions will supported. Ambient, diffuse and specular light. Ambient light is the generally background illumination, independent from the position of the light source and the view. Every object can have different material properties. According to Lambert the effective light intensity is attenuated by the cosine of the angle between the direction of the light and the direction from the light to the vertex being lighted. The specular light source contribution is the product of the material specular reflectance, the light’s specular intensity, and the dot product of the normalized vertex-to-eye and vertex-to-light vectors, raised to the power of the shininess of the material. Further more all three light source contributions are attenuated equally based on the distance from the vertex to the light source and on light source direction, spot exponent, and spot cut-off angle. This means the given factor, raised to the power of a spot exponent. Thus, higher spot exponents result in a more focused light source. If the light is positional, rather than directional, its intensity is attenuated by the reciprocal of the sum of a constant factor, a linear factor multiplied by the distance between the light and the vertex being lighted, and a quadratic factor multiplied by the square of the same distance.

4.4 Shadows

Figure 13: Volume shadow by using the stencil buffer.

Shadow calculations help the viewer to manage the scene faster. The brain get a better and faster depth impression. One the other hand the scene looks more realistic. In the computer graphic are a couple of publications, how to render a scene with shadows. In the game industry many tricks was created to calculate really fast shadows. One example is the mirroring of objects to a plane, most to the floor. But this are only possible planar shadows. More difficult are volume shadows. In this case all objects in a shadow volume becomes shadow. The idea is to mask the scene by a special buffer. Verticies will only rendered if a special buffer is confirmed to a function (LESS, GREATER, EQUAL etc.). Modern graphic adapter supports such buffer in hardware, the depth buffer and the stencil buffer are some of this. The next following steps describe how to use the stencil buffer for a fast volume shadowing. This approach was first introduced by F. Crow in 1977(Crow, 1977).

Render all verticies in the color buffer in consideration of the depth buffer. The color buffer is the final buffer we really see. The depth buffer represent the z-value (depth) of every rasterized pixel. Only one pixel in the same row and column, that with the nearest z-value to the view point must be drawn. The following next steps describe the shadow algorithm.

- Render all front faces to the stencil buffer (stencil function increment)
- Render all back faces to the stencil buffer (stencil function decrement)
- Blend shadow over the whole scene where stencil is not equal

The culling function specifies, whether front- or back-facing facets can be culled. Front and back is dependent to the order of the vertex points, counter clockwise or clockwise, mostly counter clockwise. Fig. 13 depict the workflow. Our triangle are counter clockwise, therefore the drawn rectangle one and three are also counter clockwise. This both rectangle increment the stencil buffer in the first pass. In the second pass the drawing is seted to clockwise and the stencil function to decrement the stencil buffer. Only the rectangle on edge two will drawn (decrement the stencil buffer). Now the stencil buffer is masked correctly. Finally a rectangle over the whole view will be blended. Everywhere the stencil buffer is not equal a shadow will be blended. The result is the projected shadow and shadowed objects in the shadow volume. To increase the performance we can calculate the object silhouette. This can be done by calculate the connectivity of all faces, like explain in the section connectivity. Further more the visibility of a face must be calculated, because the faces of a volumetric object e.g. a cube are always connected. In this case the algorithm draw only not connected edges of a face or when the face itself is not visibly. Of course the algorithm first can check is the object itself visible or not to increase the performance.

4.5 Texturing

Texturing, or texturmapping is the mapping of our triangles with images. Each point coordinate (x,y,z) becomes a texture coordinate (i,j). Since we have small triangles it is not necessary to rectify the images. For bigger triangles first it is necessary to rectify the mapping part of the
image, because the images are not in the same coordinate system and are perspective. Secondly we must check that the mapped triangle was seen by camera. This is the discussed raytracing step in the introduction. Actually a typical raytracing check the camera ray with each triangle for collisions. A optimized data structure and octtrees increase the performance of the algorithm. The following approach describe how to mapping the texture very easily. This approach use the distance from every triangle to the camera position of the to mapped texture. Eq. 4 reduced by the proach use the distance from every triangle to the camera raytracing check the camera ray with each triangle for collisions. A optimized data structure and octtrees increase the performance of the algorithm. The following approach describe how to mapping the texture very easily. This approach use the distance from every triangle to the camera position of the to mapped texture. Eq. 4 reduced by the term \( \mathbf{A} \cdot \mathbf{A}_x \cdot \mathbf{\tau}_d \) gives the current camera position \( \mathbf{\tau}_0 \). The orientation is not needed in this step. The distance results by Eq. 1 and the camera position to

\[
\sqrt{(r_x - r_0x)^2 + (r_y - r_0y)^2 + (r_z - r_0z)^2}. \tag{13}
\]

Now all triangles, sorted by the nearest distance, will textured and masked in the image. If a new texture coordinate already masked in the image they will not mapped. This is also a statical procedure, all texture coordinates will pre calculated and stored in a list.

5 CONCLUDING REMARKS

This paper introduce a algorithm, how to fuse laser scanning data with images of a rotating line camera. The coordinate systems of both systems and the transformation of both data sets in one common reference system (world coordinate system) are described.

The visualization of the data and different possibilities of projection are shown. For a more realistic view some light effects and shadow calculation are discussed. A fast connectivity algorithm as an base for many calculations in the computer visualization is introduced.

For fusing data of single scans, it seems to be very easily to do this with mechanical fixes and assumed that the main point of the laser scanner and the optical projection center of the panorama camera are identical. In this case the laser point and camera assignment are directly given. But our experiences was, that for bigger models with many scans we must resign our approach. The common way is, first to calculate the 3D model by using different laser scans and then mapping the color information. Triangulation and meshing of this huge unorganized pointclouds is a separate step. Many publication about this procedure are available. By using the approach from Tim Bodenmüller we generate a initial dense mesh. In future work we must more simplify this mesh. Errors in the mesh e.g. holes must be found automatical.

Texturemapping with the panoramic data are shown. The radiometric problems by mapping different textures must also research in future work. A homogeneous lightning with different camera placements during the data acquisition is very difficult. Shadows caused by real light must be found automatical and must be modified radiotmetrical or masked for not using.

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