

MAKE WIDE-ANGLED AERIAL CAMERA BY COMBINING SMALL-SIZED AREAL ARRAY CCD SENSORS

WenLing Xuan^{*a}, Dong Wang^b, Jie Sun^c

^a Information Institute, Wuhan Univ., 129 LuoYu Rd. Wuhan, Hubei Prov. PRC, 430079;

^b College of Geo-inf. Science & Engineering, Shandong Univ. of S&T, Tai'an, Shandong Prov. PRC, 271019;

^c Chinese Academy of Surveying & Mapping, 16 BeiTaiPing Rd. Beijing, PRC, 100039

paper_nstl@yahoo.com.cn fax 86 10 68181834

ABSTRACT

A new method for combining small-sized areal array CCD sensors to make one wide-angled digital aerial photography system is studied in this paper. The method is to install several small-sized areal array CCD cameras in the way that their perspective projecting centers form a line or a square, with their principal optical axes slanting fixed angle along designed directions. Such installation aims at getting one big frame of image, which is the exact mosaic of group image captured by combined cameras at one time, equivalent to the one taken directly by a wide-angled aerial camera. The system parameters: position relationships between cameras, exact principal distance of each camera and optical distortion parameters of each lens are obtained with high precision through our designed camera calibration method – space resection with several images of calibration field. The research work and experiments in this paper can guide the production of whole wide-angled high-resolution digital camera.

Keywords: wide-angle digital camera, multi-camera system, equivalent image, camera calibration, high resolution aerial image.

1. INTRODUCTION

Due to the limitation of technical level, the size of current areal CCD sensor is not big enough to be used to make the high-resolution wide-angled aerial camera. Although it is no problem to make the normal-angled camera with CCD sensor of normal size, if using it to capture high-resolution image, its shortcoming of too small imaging size causes the problem - the necessary image overlapping area required in conventional aerial photography is hard to keep under the limited flying control condition of nowadays. As illustrated in Fig. 1, in terms of same flying control precision, big images in Fig. 1_a are able to meet the overlapping requirement, while small images shown in Fig. 1_b can even hardly reach the requirement of seamless overlay.

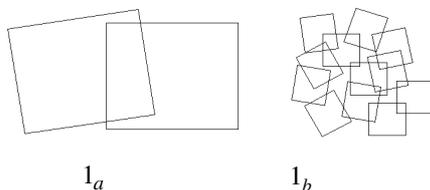


Fig. 1: Flying control error affects image overlap

On the one hand, what we have is small-sized areal CCD camera; on the other what we desire is large-sized high-resolution aerial image. In order to solve this dilemma, this paper presents a method using small-sized CCD sensors to

compose the wide-angled aerial camera.

2. MULTI-CAMERA COMBINED AERIAL PHOTOGRAPHY SYSTEM

The wide-angled high-resolution aerial photography system made from multi-camera combination may have 3-camera and 4-camera structure. This part studies the two types of structure, equivalent image converting etc. in detail.

2.1 3-camera combination scheme

1). Structure

The 3 small-sized cameras are laid out on the airplane's platform in the following way (Fig. 2): the projecting centers of the three camera (S_2, S_1, S_3) are in one line, parallel to airplane's platform and to flying direction. The distance between two adjacent camera's projecting centers is ΔS_x . The middle camera S_1 has its principal optical axis SO_1 perpendicular to airplane's platform, the second camera S_2 's principal optical axis SO_2 is vertical to flying direction but tilts left a certain angle from SO_1 , and the third camera S_3 's principal optical axis SO_3 is vertical to flying direction but tilts right a certain angle from SO_1 . In this case, if there is a set of parallel lines on the ground and they are vertical to flying direction, the respective image formed in the 3 cameras will be as Fig. 3 shows. That is, image of the middle camera is parallel lines. Image of the second camera (left-tilt camera) is left convergent lines and the main vanishing point is I_2 . Image of the third camera (right-tilt camera) is right

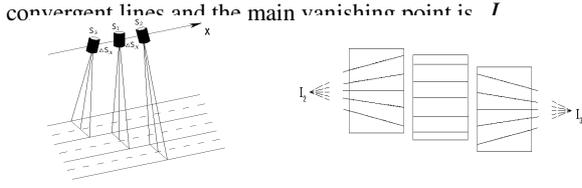


Fig. 2: Layout of 3 cameras Fig.3: Parallel lines' image in 3 cameras

2). Image conversion in 3-camera system

Generally, the three images can be transformed into the horizontal equivalent image P_0 through the algorithm given below. The transformation principle is illustrated in Fig. 4, where 3 cameras' projecting centers are virtually overlapped into one point S , along flying direction. Signs θ_2, θ_3 denote the tilt angles of P_2, P_3 . Signs f_2, f_1, f_3 and f_0 denote the principal-distances of P_2, P_1, P_3 and the equivalent image P_0 respectively. The captured images are in the position of P_2, P_1, P_3 (left-tilt P_2 , horizontal P_1 and right-tilt P_3).

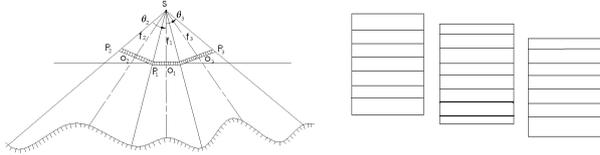


Fig. 4 Illustration of images conversion Fig.5: projecting center displacement

Assume that the flying direction is X coordinate axis. ΔS_x is the projecting center displacement between two adjacent camera, i.e. S_2 and S_1, S_3 and S_1 . Then, according to the principle of collinear equation, the transforming expression from P_1 to P_0 is

$$\begin{cases} x_0 = f_0 \frac{x_1}{f_1} \\ y_0 = f_0 \frac{y_1}{f_1} \end{cases} \quad (2-1)$$

The transforming expression from P_2 to P_0 is:

$$\begin{cases} x_0 = f_0 \frac{x_2}{y_2 \sin \theta_2 + f_2 \cos \theta_2} + \Delta S_x \\ y_0 = f_0 \frac{y_2 \cos \theta_2 - f_2 \sin \theta_2}{y_2 \sin \theta_2 + f_2 \cos \theta_2} \end{cases} \quad (2-2)$$

The transforming expression from P_3 to P_0 is:

$$\begin{cases} x_0 = f_0 \frac{x_3}{y_3 \sin \theta_3 + f_3 \cos \theta_3} - \Delta S_x \\ y_0 = f_0 \frac{y_3 \cos \theta_3 - f_3 \sin \theta_3}{y_3 \sin \theta_3 + f_3 \cos \theta_3} \end{cases} \quad (2-3)$$

Because practically, we are unable to position 3 cameras' projecting centers at exactly the same point in space, the projecting center displacement (See Fig.5) from second and third camera to middle camera ΔS_x needs to be added to

formula (2-2) and subtracted from (2-3).

In 3-camera combination scheme, the field of view (FOV) of whole photography system is enlarged 3 times of a single camera in the direction vertical to flight. But the FOV along flying direction remains no change (Actually it shrinks.). So the longitudinal overlap should be increased in the course of aerial photography. In general, it is easier to control longitudinal overlap than lateral overlap. Hence, this method is practicable.

2.2 4-camera combination scheme

1).Structure

Other than the structure of 3-camera combination, in the 4-camera combination scheme, each camera ought to tilt outwards a certain angle so that the overall FOV is expanded in both X and Y directions. That is, each camera has to rotate angles θ_x, θ_y round X, Y coordinate axis respectively, as shown in Fig. 6_a, 6_b. In such a structure, the 4 cameras' projecting centers form a square, with their principal optical axes tilting fixed angle along designed directions.

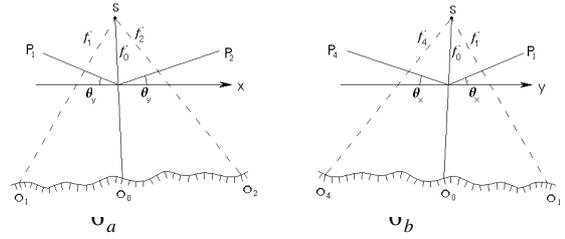


Fig. 6: Camera tilt in 4-camera combination scheme

The geometry shape of the 4 original images from 4-camera system is like the solid lines in Fig. 7. And after the rectification of them and mosaic them, the equivalent image is like the dash lines in Fig. 7. It shows that the virtual principal optical axis of the equivalent image P_0 is perpendicular to horizontal plane, while the four actual principal optical axes corresponding to the four cameras are biased $\pm\theta_x, \pm\theta_y$ from the virtual principal optical axis. Fig. 8 shows the analytical expression of $\vec{\theta}_x, \vec{\theta}_y$ in vector form.

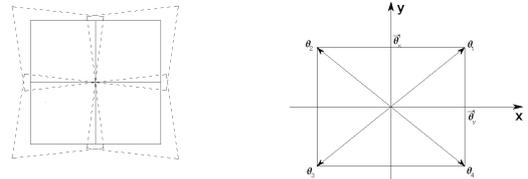


Fig. 7: Original and equivalent images Fig. 8: Bias of actual principal optical axes

2). Image conversion in 4-camera system

The image conversion from P_1, P_2, P_3 and P_4 into P_0 consists of the rectification of image tilt and the correction

of projecting center shifts. The principal of tilt rectification is

$$\begin{bmatrix} x_0 \\ y_0 \\ -f_0 \end{bmatrix} = \begin{bmatrix} \cos\theta_y & 0 & \sin\theta_y \\ 0 & \cos\theta_x & \sin\theta_x \\ -\sin\theta_y & -\sin\theta_x & \cos\theta_x \cos\theta_y \end{bmatrix} \begin{bmatrix} x \\ y \\ -f \end{bmatrix}$$

that is,

$$\begin{cases} x_0 = -f_0 \frac{x \cos\theta_y - f \sin\theta_y}{-x \sin\theta_y - f \sin\theta_x + f \cos\theta_x \cos\theta_y} \\ y_0 = -f_0 \frac{y \cos\theta_x - f \sin\theta_x}{-x \sin\theta_y - y \sin\theta_x + f \cos\theta_x \cos\theta_y} \end{cases}$$

Add the correction value $\Delta S_x \Delta S_y$, then

$$\begin{cases} x_0 = -f_0 \frac{x \cos\theta_y - f \sin\theta_y}{-x \sin\theta_y - f \sin\theta_x + f \cos\theta_x \cos\theta_y} - \Delta S_x \\ y_0 = -f_0 \frac{y \cos\theta_x - f \sin\theta_x}{-x \sin\theta_y - y \sin\theta_x + f \cos\theta_x \cos\theta_y} - \Delta S_y \end{cases}$$

□. MULTI-CAMERA SYSTEM CALIBRATION

The design in part 2 actually is an ideal situation that no error occurs during the process of system manufacture and assembly. However, the system error is inevitable. The real wide-angled photography system made of combined small-sized CCD cameras needs system calibration of high precision. The parameters to be calibrated ought to include:

- 1) Each camera's inner elements (x_0, y_0, f_0) and optical distortion parameters.
- 2) Relative exterior elements $(\theta_x, \theta_y, \theta_z, dS_x, dS_y, dS_z)$ in combination system.

3.1 Indoor and outdoor calibration field

In order to carry out the required calibration, we utilize both indoor (Fig. 9) and outdoor (Fig. 10) calibration field, which are built specially for the purpose of close-range camera calibration. Within the two calibration fields, controlling points array with rather big space depth are arranged. The coordinates of them are precisely determined by geodetic instrument and are checked for deformation correction caused by varied environment conditions periodically. So the coordinates values of controlling points in our calibration field can be used as true value in system calibration.

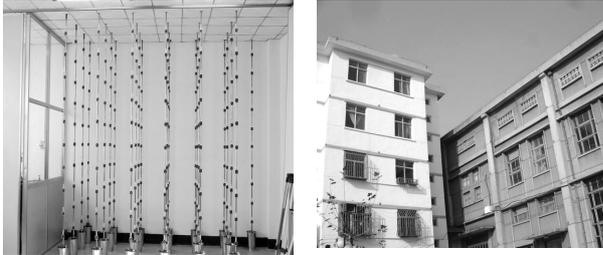


Fig. 9: Indoor calibration field Fig. 10: Outdoor calibration field

3.2 Principle and algorithm of camera calibration

To peel off the correlative influence between inner and exterior elements (including distortion parameters), we specially designed the solution called space resection with multiple images. The method uses several images that cover a certain number of controlling points of calibration field, takes the coordinates of controlling points in image as observation value, solves exterior elements, optical distortion errors, other parameters affecting light beam shape as well as exterior elements of multi-images as a whole, on the basis of collinear equation, with the controlling points' coordinates in object space taken as true value.

Denote exterior elements as X_{ex} , inner elements of image as X_{in} , some added parameters as X_{ad} , observation values as V . According to collinear equation in photogrammetry, the error equation can be written as:

$$V = AX_{ex} + BX_{in} + CX_{ad} - L$$

Where, the denotations carry the following matrix expressions:

$$V = \begin{bmatrix} v_x \\ v_y \end{bmatrix}^T \quad X_{in} = [\Delta f \quad \Delta x_0 \quad \Delta y_0]^T$$

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} & a_{16} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} & a_{26} \end{bmatrix}$$

$$C = \begin{bmatrix} \bar{b}_1 & \bar{b}_2 & \cdots & 0 & 0 & \cdots \\ 0 & 0 & \cdots & c_1 & c_2 & \cdots \end{bmatrix}$$

$$X_{ex} = [\Delta X_s \quad \Delta Y_s \quad \Delta Z_s \quad \Delta \varphi \quad \Delta \omega \quad \Delta \kappa]^T$$

$$X_{ad} = [a_1 \quad a_2 \quad \cdots \quad \beta_1 \quad \beta_2 \quad \cdots]^T$$

$$B = \begin{bmatrix} a_{17} & a_{18} & a_{19} \\ a_{27} & a_{28} & a_{29} \end{bmatrix} \quad L = [x - (x) \quad y - (y)]^T$$

Suppose three images I□II□III are captured, and each one possesses the communal points 1,2, ...n and has four added

parameters $a_1 \square a_2 \square \beta_1 \square \beta_2$, then the error equation is

$$V = \begin{matrix} A & X_{ex} & B & X_{in} & C & X_{ad} & -L \\ 6n \times 1 & 6n \times 18 & 6n \times 3 & 6n \times 3 & 6n \times 4 & 6n \times 4 & 6n \times 1 \end{matrix}$$

That is,

$$V = \begin{bmatrix} A_{E-1} & 0 & 0 & B_{E-1} & C_{E-1} \\ \dots & \dots & \dots & \dots & \dots \\ A_{E-n} & 0 & 0 & B_{E-n} & C_{E-n} \\ 0 & A_{I-1} & 0 & B_{I-1} & C_{I-1} \\ \dots & \dots & \dots & \dots & \dots \\ 0 & A_{I-n} & 0 & B_{I-n} & C_{I-n} \\ 0 & 0 & A_{II-1} & B_{II-1} & C_{II-1} \\ \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & A_{II-n} & B_{II-n} & C_{II-n} \end{bmatrix} \begin{bmatrix} X_{E-ex} \\ X_{IE-ex} \\ X_{IIE-ex} \\ X_{in} \\ X_{ad} \end{bmatrix} = \begin{bmatrix} x_{E-1} - (x_{I-1}) \\ \dots \\ y_{E-n} - (y_{I-n}) \\ x_{I-1} - (x_{II-1}) \\ \dots \\ y_{I-n} - (y_{IIE-n}) \\ x_{II-1} - (x_{IIE-1}) \\ \dots \\ y_{IIE-n} - (y_{IIE-n}) \end{bmatrix}$$

According to the least square principle: $V^T \times V = \min$, so the unknown parameters X_{IE-ex} , X_{IIE-ex} , X_{in} and X_{ad} can be solved by the following iterative process:

$$\begin{bmatrix} X_{E-ex} \\ X_{IE-ex} \\ X_{IIE-ex} \\ X_{in} \\ X_{ad} \end{bmatrix} = \left(\begin{bmatrix} A & 0 & 0 & B & C \\ 0 & A_I & 0 & B_I & C_I \\ 0 & 0 & A_{II} & B_{II} & C_{II} \end{bmatrix} \right)^{-1} \begin{bmatrix} x_{E-1} - (x_{I-1}) \\ \dots \\ y_{I-n} - (y_{IIE-n}) \end{bmatrix}$$

3.3 Calibration contents in multi-camera system

Though the principle and technique of CCD cameras is quite different from that of common analog cameras, the two categories are similar in calibration specifications and method. However, the calibration contents vary from different purposes. As for our multi-camera system, the following items are calibrated first: The inner elements of each camera: principal point x_0, y_0 and principal distance f ; The optical distortion parameters: radial distortion factors k_1, k_2, \dots and eccentric distortion factors p_1, p_2 .

After the inner elements and distortion parameters of each small-sized CCD camera has been obtained using the solution of space resection with multiple images, the cameras are mounted onto the platform specially designed for multi-camera combination system and they are electronically controlled to take the images of the same calibration field simultaneously. With these data, real exterior elements: linear elements X_S, Y_S, Z_S and angle elements φ, ω, κ of the multi-camera system, relative exterior elements of each camera to the principal optical axis of equivalent image $(\theta_x, \theta_y, \theta_z, dS_x, dS_y, dS_z)$ are to be determined.

3.4 Multi-camera system correction

The following corrections are indispensable for practical system. The corrections are based on system calibration results.

1) Exterior elements correction

The correction component of exterior elements $(dS_x, dS_y, dS_z, d\theta_x, d\theta_y, d\theta_z)$ is the difference between system design value and its corresponding calibrated value.

2) Image coordinates correction

Denote corrected image coordinates as (x', y') , observed image coordinates as (x_{im}, y_{im}) , radial distortion factor as k_1 . (Since our multi-camera system use small-sized non-metric CCD cameras, we can take the radial distortion factor k_1 into consideration only.) Suppose r is the radius from image point to principal point. Then correction model for image correction is:

$$\begin{cases} x' = x_{im} - x_0 + k_1 (x_{im} - x_0) r^2 \\ y' = y_{im} - y_0 + k_1 (y_{im} - y_0) r^2 \end{cases}$$

$$\text{Where, } r^2 = (x_{im} - x_1)^2 + (y_{im} - y_1)^2$$

3) Equivalent image correction

The equivalent image coordinates (x, y) is calculated on the basis of (x', y') . Further, (x, y) needs to be corrected by correction component of exterior elements. The correction equation is:

$$\begin{cases} dx = ds_x + \frac{x}{f} ds_z + (f + \frac{x^2}{f}) d\theta_y + \frac{xy}{f} d\theta_x + y d\theta_z \\ dy = ds_y + \frac{y}{f} ds_z + (f + \frac{y^2}{f}) d\theta_x + \frac{xy}{f} d\theta_y + x d\theta_z \end{cases}$$

□.EXPERIMENTS

The following experiments are carried out to test and verify the above mentions.

Four FUJIFILM FinePix 4700zoom areal CCD cameras are used in the experiments. FinePix type is characterized by small size, handy use, high light sensitivity, large storage etc..especially, the capability of locking principal distance.

3 and 4 FinePix 4700zoom cameras are mounted on experimental multi-camera platform to construct the 3-camera combination system (Fig. 12) and 4-camera combination system (Fig. 13).

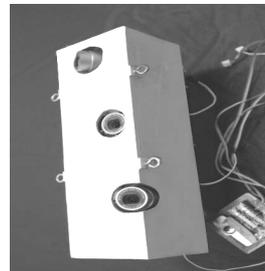


Fig. 12: 3-camera system

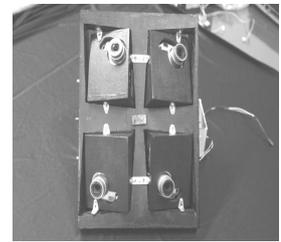


Fig. 13: 4-camera system

Table 1 gives the result for each single camera calibration. The calibration is done through outdoor

calibration field, employing the method of space images are used.)
 resection with multiple images.(For each camera, 4

Table 1: Single FinePix 4700zoom camera calibration result.

		CAMERA I	CAMERA II	CAMERA III	CAMERA IV
Image No. 1	X_c (m)	1015.198	1013.998	1013.889	1013.604
	Y_c (m)	205.855	205.995	205.887	205.947
	Z_c (m)	-499.199	-500.222	-500.151	-500.271
	ϕ (dms)	-49.3450	-52.5359	-50.2327	-50.2122
	ω (dms)	21.5354	22.5656	24.3053	24.3908
	κ (dms)	-1.5025	-1.4629	-3.0603	-6.2600
Image No. 2	X_c (m)	1015.067	1013.866	1013.771	1013.412
	Y_c (m)	205.861	205.822	205.949	205.812
	Z_c (m)	-499.029	-500.163	-499.993	-500.185
	ϕ (dms)	-55.2224	-57.5505	-52.0226	-51.5416
	ω (dms)	22.0429	22.3040	24.3618	22.4853
	κ (dms)	87.4625	85.5028	86.4004	83.0528
Image No. 3	X_c (m)	1017.916	1015.769	1015.682	1015.908
	Y_c (m)	205.913	206.025	205.925	205.956
	Z_c (m)	-504.104	-504.228	-504.560	-504.341
	ϕ (dms)	-65.2017	-64.1110	-62.4347	-62.1503
	ω (dms)	20.4813	22.1640	23.5959	25.5026
	κ (dms)	0.0851	-0.4715	-0.4551	-2.4304
Image No. 4	X_c (m)	1017.863	1015.706	1015.623	1015.809
	Y_c (m)	205.906	205.859	205.948	205.834
	Z_c (m)	-503.990	-504.106	-504.418	-504.226
	ϕ (dms)	-71.4651	-69.1735	-63.5131	-64.1245
	ω (dms)	23.4640	24.5841	24.3252	23.1752
	κ (dms)	88.34050	87.1827	88.1544	84.4937
x_0 (p)		6.22	-24.03	38.95	1.26
y_0 (p)		0.79	19.37	21.75	40.84
f (p)		2690.33	2675.15	2727.05	2689.32
k_1 (p ⁻²)		-4.03e-008	-4.15e-008	-3.77e-008	-3.86e-008

Notes:

- 1.The above parameters units: *m* stands for meter, *dms* for degree minute second, *p* for pixel, *p*⁻² .for pixel⁻²
- 2.The calibrated parameters of x_0 , y_0 f are in pixel. To convert them into millimeters, multiply the size of each pixel.
- 3.The calibrated result is applicable for infinite distance.

The calibrations of 4-camera system and 3- camera system are also done through indoor calibration field. The image is got by electronically controlling 4 or 3 cameras to expose at the same time. Two sets of image data is used.. Due to space limitation in space, the data is not included in the paper..

The Unmanned Aerial Vehicle (UAV-II, developed by Chinese Academy of Surveying&Mapping, Fig. 14) has equipped with 3-camera system to take aerial images of Beijing suburb. Fig.15 is one image product of 3-camera system. It is the equivalent image from 3 single images' recitification and mosaic with cooresponding algorithms.



Fig.14: UAV-II equipped with multi-camera system



Fig. 15: One equivalent image of 3-camera

□.CONCLUSION

Based on the research work and experiments in this paper, we have the following application ideas:

- 1.To construct multi-camera system using the common simple digital cameras. To equip simple Unmanned Aerial Vehicle equipped with such aerial camera to make low-altitude aerial photography will get high-resolution aerial images.
- 2.Guided by the researched principle, the whole camera with 3 or 4 lens and corresponding aeral CCD sensors can be developed. To perform precise calibration of such whole camera in factory in order that the inner and exterior elements approach theoretic design values to the utmost. Then wide-angled high-resolution digital camera is produced.

REFERENCES

- 1.Zhizhuo Wang, *principle of photogrammetry*, Publishing House of Surveying and Mapping,Beijing,1979
- 2.Wenhao Feng, *Close-range photogrammetry*, Publishing House of Wnhan Univ.Wuchang, 2002
- 3.Wenhao Feng,, *Deduction of Constraint Condition in the Calibration of Stereo-Vision System*. Journey of Wuhan Technical Univ. of Surveying & Mapping, Vol.1, No.1, 1998
- 4.Axel Graser, *Synchronization of a Stereo Camera System for Auto-Zoom in the Rehabilitation Robot FRIEND*,
- 5.Fraser,C.S. *Some Thoughts on the Emergence of Digital Close-Range Photogrammetry*. The Photogrammetric Record, Apr.1998
- 6.FUJI Photo Film Co.,Ltd., *Owner's ManualFUJIFILM Digital Camera FinePix 4700zoom*, Japan,2001.