

AUTOMATIC CLASSIFICATION OF CENTRAL ITALY LAND COVER: COMPARATIVE ANALYSIS OF ALGORITHMS

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ABSTRACT:

The specific objective of this paper was to provide a comparative analysis of three automatic classification algorithms: Quinlan's C4.5 and two robust probabilistic classifiers like Support Vector Machine (SVM) and AdaBoost (a short for "adaptive boosting"). This work is part of a wider project whose general objective is to develop a methodology for the automatic classification, based on CORINE land-cover (CLC) classes, of high resolution multispectral IKONOS images. The dataset used for the comparison is an area of approximately 150 km² comprising both urban and rural environments. Input data are basically constituted by multispectral (red, green, blue and infrared bands), 4m ground-resolution images. In some classifications they are integrated by the Normalized-Difference-Vegetation-Index (NVDI), derived from the red and infrared bands, a Digital Terrain Model (DTM) of the area and pixel by pixel gradient values, derived by the DTM. All the above algorithms had to perform full data classification into four classes: vegetation, water bodies, bare soil, and artificial cover. The output is constituted by an image with each pixel assigned to one of the above classes or, with the exception of C4.5, left unclassified (somehow a better solution than a classification error). In addition, a confusion matrix for control data is produced to evaluate the accuracy of each algorithm, by computing the percentage of correctly classified pixels with respect to the total number of pixels, the user's and producer's accuracy indexes and the Cohen's coefficient to evaluate global accuracy. Even if an optimal distribution of the samples in the training set has a great influence, results demonstrate the suitability of supervised classifiers for high resolution land cover classification. In particular, all the proposed approaches work fine, so that we are now exploring the use of more classes, that is at the second level of the CORINE legend.

1. INTRODUCTION

The concept of classification is based on the following definition: given a set of observations of a concept, the learner induces a general concept description that covers the instances observed. The best is the generalization from learning data to test data, the better is the classificatory performances.

Classification has been used in several fields: from robotics to genetics, from document classification to vision and risk management (Wood 1996), (Burges, 1998), (Meyer 2003). Image classification for the production of thematic maps, such as those depicting land cover, is one of the most common applications of remote sensing. In fact, the land cover maps derived are often judged to be of insufficient quality for operational applications, due to disagreements between the derived land cover map and some ground or other reference dataset. Consequently, an updating of these maps must be carried out on a regular basis to keep the databases up to date.

This work is part of a wider project whose general objective is to develop a methodology for the automatic classification, based on CORINE land-cover classes (EEA, 2008), of high resolution multispectral IKONOS images.

The whole project was divided into four stages consisting of:

- i) pre-processing – the image dataset has been orthorectified with respect to a chosen coordinate system;
- ii) definition of training and control sample sets – an exhaustive number of samples, based on a hierarchical classification nomenclature, is the base for the training of algorithms and for accuracy assessment. The spectral analysis of the different channels of the image has been also

carried out to select optimal bands or combination of bands, to be used in the classification process;

- iii) classification – different supervised classification methods were tested;
- iv) accuracy assessment of classification results – an estimate of the accuracy of different classifications was carried out.

The specific objective of this paper was to provide a comparative analysis of three automatic classification algorithms: Quinlan's C4.5 and two robust probabilistic classifiers like SVM and AdaBoost.

The case study refers to an area of approximately 150 km² belonging to the Ancona province of the Marche region in Italy (Figure 1). The images were provided thanks to a research agreement signed between Regione Marche, a regional institution of central Italy, and three departments (DARDUS, DIIGA and DiSASC) of the Polytechnic University of Marche.

In the rest of this section we describe the CLC legend for land cover classification, in Section 2 the definitions of the analysed automatic classification algorithms, in Section 3 we present the results obtained, and in Section 4 comments and conclusions.

1.1 Land cover classification: CLC legend

In 1985 the European Commission approved the CORINE programme, led by the European Environmental Agency in coordination with the member countries, to compile, in a consistent and compatible way, information on certain topics with regard to the state of the environment. Among the results there was the definition of CORINE Land Cover inventories for all European countries, at the scale of 1 : 100,000, based on a

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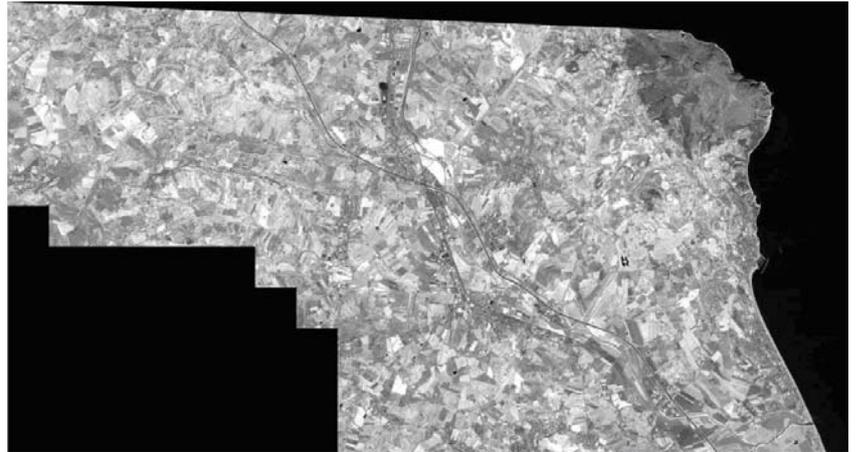


Figure 1. Case study: Italy, Marche region, Ancona province. On the right a panchromatic image of the area that has been processed.

standard methodology and nomenclature, for use with remote sensing techniques. The CLC legend has a hierarchical structure on three levels, containing 44 land cover classes grouped into five major categories: 1. Urban Fabric, 2. Agriculture areas, 3. Forest and semi-natural areas, 4. Wetlands, 5. Water bodies. With respect of this structure, the high ground resolution of current sensors, suitable for a map scale 1:10,000, suggested the introduction of fourth and fifth level categories.

2. AUTOMATIC CLASSIFICATION ALGORITHMS

In this section, we describe the main classification methods that will be used in this paper. We start by formally defining the classification problem. Assume that we are given a training set D , consisting of pairs $\langle x_i, l_i \rangle$, for $i=1,2, \dots, m$. Each sample x_i is a vector in R^m that describes features joined to a certain concept. The label l_i associated with x_i is a binary or a multiple label (for simplicity, we will discuss two-label classification problems that can be easily generalized). A classification algorithm is a function F that depends on two arguments, the training set D and a query about x_q that returns a predicted label l_q . We also allow for no classification to occur if x_q is either close to none of the classes or when it is too borderline for a decision to be taken. Formally, this is realized by allowing the label l_q to be 0, 1 or 2, the latter representing an unclassified query. Good classification procedures predict labels that typically match the “true”, intended as ground truth, label of the query. When unclassified is accepted as a possible output one needs to consider the costs/penalties of the various outcomes in analyzing the value of a classification method.

In our case $\langle x_i, l_i \rangle$ are respectively a set of feature coming from pixel based or region based analysis of multispectral images joined, in some cases, with other pixel or region specific characteristics (e.g. altitude, exposition, etc.).

Here following we give a brief description of the three proposed and tested classification methods: Quinlan’s C4.5, Support Vector Machine (SVM) and AdaBoost.

2.1 - C4.5

The machine learning community has produced a large number of programs to create decision trees for classification. Noteworthy are Quinlan’s C4.5 (Quinlan, 1993), which is a descendant of his earlier program ID3, and CART -

Classification And Regression Trees (Breiman, 1984), which is a sophisticated program for fitting trees to data.

In general, tree-structured classifiers are constructed by making repetitive splits of the measurement space X and the subsequently created subsets of X , so that a hierarchical structure is formed. It should be noted that when X is divided into two subsets, these subsets do not both have to be subsequently divided using the same variable, allowing modelling a non homogeneous response. Besides, the classification trees produced by tree-structured classification methods are not guaranteed to be optimal: at each stage in the tree growing process the split selected is the one that will immediately increase the node purity the most (all cases from the learning sample corresponding to the node belonging to the same class); that is, on the contrary of using a tree-growing program that “looks ahead”, which would require much more time to create a tree, they are greedy algorithms.

C4.5 is a quite standard Decision Trees (Breiman, 1984) used as general purpose learning technique for supervised classification; it produces a flow chart like tree structure where each node denotes a test on an attribute. Each branch represents an outcome of the test and leaf nodes represent classes or class distributions. In general the decision tree approach has several disadvantages (multiple trees, variations) and the main advantages are effectiveness and efficiency.

The basic algorithm to build decision trees uses a greedy algorithm that constructs the tree starting from the top and then goes down recursively by divide and conquer manner. C4.5 uses sophisticated pruning, and probabilistic facilities are used to handle unknown and imprecise attribute values; unlike basic approaches, C4.5 selects a working set of examples at random from the training data and then tree growing/pruning process is repeated several times to ensure that the most promising tree has been selected.

2.2 - Support Vector Machine (SVM)

Support vector machines (SVMs) are a set of related supervised learning methods used for classification and regression. They belong to a family of generalized linear classifiers. They can also be considered a special case of Tikhonov regularization. A special property of SVMs is that they simultaneously minimize the empirical classification error and maximize the geometric margin; hence they are also known as maximum margin classifiers.

Support vector machines map input vectors to a higher dimensional space where a maximal separating hyperplane is constructed. Two parallel hyperplanes are constructed on each side of the hyperplane that separates the data. The separating hyperplane is the hyperplane that maximizes the distance between the two parallel hyperplanes. An assumption is made that the larger the margin or distance between these parallel hyperplanes the better the generalisation error of the classifier will be. A tutorial has been produced by C.J.C Burges (Burges, 1998). A comparison of SVM to other classifiers has been made by Meyer et al. (2003). An assessment of SVMs for land cover classification is in Huang et al. (2002).

2.3 - AdaBoost

Boosting (Sutton, 2005) is a method of combining classifiers, each of which iteratively created from weighted versions of the learning sample, with the weights adaptively adjusted at each step to give increased weight to the cases that were misclassified on the previous step. The final predictions are obtained by weighting the results of the iteratively produced predictors. Boosting was originally developed for classification, and is typically applied for creating an accurate strong classifier by combining a set of weak classifiers. A weak classifier is only required to be better than chance, and thus can be very simple and computationally inexpensive. However, combining many of them results in a strong classifier, which often outperforms most "monolithic" strong classifiers such as SVMs and Neural Networks. In 1990 Schapire (Schapire, 1990) developed the predecessor to later boosting algorithms developed by him and others. AdaBoost (a short for "adaptive boosting") is now the most popular boosting algorithm (Freund, 1997). Different variants of boosting are known such as Discrete Adaboost, Real AdaBoost, and Gentle AdaBoost (Schapire 1999). All of them are identical with respect to computational complexity from a classification perspective, but differ in their learning algorithm. As already said, boosting uses a weighted average of results obtained from applying a prediction method to various samples, but the samples used at each step are not all drawn in the same way from the same population, rather the incorrectly predicted cases from a given step are given increased weight during the next step. Thus boosting is an iterative procedure, incorporating weights, as opposed to being based on a simple averaging of predictions, as is the case with bagging (Sutton, 2005). In addition, boosting is often applied to weak learners (e.g., a simple classifier such as a two node decision tree), whereas this is not the case with bagging.

AdaBoost is an algorithm for constructing a "strong" classifier as the linear combination

$$f(x) = \sum_{t=1}^T \alpha_t h_t(x)$$

of simple weak classifiers $h_t(x)$, which can be seen as basis classifier, hypothesis or features. The strong classifier H derives from the sign evaluation of the weak classifiers:

$$H(x) = \text{sign}(f(x))$$

The modified Real AdaBoost algorithm can be sketched as:

Modified Real AdaBoost algorithm

Input: Set of N labelled examples $(x_1, y_1), \dots, (x_N, y_N)$, with $y_i \in \{-1, 1\}$, for $1 \leq i \leq N$, $x_i \in \mathfrak{R}^k$, and where $y_i = +1$ for positive examples and $y_i = -1$ for negative examples. x_i is a feature vector with k -components, each encoding a feature relevant for the learning task.

Initialize weights $D_1(i) = 1/N$

for $t = 1, \dots, T$ **do**

1. Call the weak classifier $h_t(x_i)$ that returns the minimum error with respect to the distribution D_t ;

It returns weak classifier $h_t : X \in \{-1, 1\}$ from $H = \{h(x)\}$ according to the following error function:

$$h_t = \arg \min_{h_j \in H} \varepsilon_j = \sum_{i=1}^m D_t(i) [y_i \neq h_j(x_i)]$$

2. Update $D_{t+1}(i) = \frac{D_t(i) * e^{-\alpha_t y_i h_t(x_i)}}{z_t}$

where z_t is a normalization factor chosen so that D_{t+1} is a distribution.

3. Choose the weight $\alpha_t \in \mathfrak{R}$, so to greedily minimize Z_t in each step

end for

Output: The final strong classifier:

$$H(x) = \text{sign}\left(\sum_{t=1}^T \alpha_t h_t(x)\right)$$

It is important to notice that the complexity of the strong classifier depends only from the weak classifiers.

The algorithm repeatedly selects a weak classifier $h_j(x)$ using a distribution D over the training examples. The selected weak classifier is expected to have a small classification error on the training data. The idea of the algorithm is to modify the distribution D by increasing the weights of the most difficult training examples in each round. The final strong classifier H is a weighted majority vote of the best T weak classifiers.

To deal with non binary results we used a chain of binary classifier. A binary classifier C_i classifies data x into belonging to either class H^i_0 or class H^i_1 (i.e. false or positive classification). We assume each classifier C_k passes through data that it classifies as belonging to class H^i_0 only (this approach is also named filtering classifier). In this way we obtain a n -class classifier starting from a binary one.

3. RESULT AND DISCUSSION

In this section, after a brief description of the dataset and of the pre-processing operations, and the definition of the performance measures, we report and comment the classification results for the C4.5, SVM and Adaboost algorithms.

3.1 - Dataset, pre-processing and sample definition

The dataset used for the comparison is an area of approximately 150 km², located near the Ancona city, comprising both urban and rural environments, and with a topography that includes flat areas, but also the Natural Park of the Conero mountain, with a 550 m elevation range.

IKONOS images were acquired in July 2006, with a 29 degrees solar zenith angle. The dataset is composed by a panchromatic image at a ground resolution of 1m and multi-spectral 4m resolution data constituted by four bands: red, green, blue and near-infrared. These data were integrated by a Digital Terrain Model (DTM) of the area, derived from the Regional Technical Map (CTR) at the scale 1:10,000, which, however, by definition, does not consider artificial structures. In addition, in some classifications we used pixel by pixel gradient values, derived by the DTM, and the Normalized Difference

Vegetation Index (NVDI) derived from the red (r) and near-infrared (nir) channels, according to the following formula:

$$NDVI = \frac{nir - r}{nir + r}$$

During the pre-processing phase, first all the images were orthorectified in the UTM N33 WGS84 System, using a rational function model. Then a geometric correction was performed using 15 control points and the third order degree polynomial equations, giving an RMS error below 1 pixel (1 meter). A radiometric interpolation by means of the nearest neighbour re-sampling method preserved the original image values. Finally, the study area was extracted from a submap of the original image.

A classification system should be informative, exhaustive and separable (Jensen 1996, Landgrebe 2003). The first step to this aim is the definition of a hierarchical classification structure, principally based on the user's needs and spatial resolution of remotely sensed data. To fit a standard classification system we planned to use the CLC legend, but adopting the extended legend provided by the Italian agency for environmental protection and technical services (Agenzia per la Protezione dell'Ambiente e per i servizi Tecnici - APAT) for the Agriculture areas and introducing new levels, based on the spectral response of different materials, for Urban areas.

On the base of this structure, a sufficient and significant number of training samples have to be defined. The software training stage was carried out by means of about 100,000 sample points grouped in 130 training sites. After a dedicated-GIS platform implementation each sample was collected by means of specific in field campaign and/or pan-sharpened IKONOS dataset visual interpretation. The choice of the detail level of the samples (i.e., if belonging to the first or to the second level of the legend) was carried out by class separability statistical measurements. This also allowed to improve the training set by excluding sites with spectral values largely ranging far from corresponding class mean values.

3.2 - Performance measures

We decided to analyse all the three classification algorithms while performing full data classification at the first level of our land cover legend, that is, into four classes: vegetation (V), artificial cover (A), water bodies (W) and bare soil (B). The output is constituted by an image with each pixel assigned to one of the above classes or, with the exception of C4.5, let unclassified (somehow a better solution than a classification error).

The quantitative evaluation of the accuracy of each algorithm was made according to the values of the confusion matrixes (Foody, 2002) resulting from control data classification. In particular, each confusion matrix is constituted in our case by the labels of the four classes plus the user's accuracy index (UA) as last column attribute and the label NC, corresponding to not-classified pixels, plus the producer's accuracy index (PA) as further row attributes:

	V	A	W	B	UA
V	X_{11}	X_{12}	X_{13}	X_{14}	UA_V
A	X_{21}	X_{22}	X_{23}	X_{24}	UA_W
W	X_{31}	X_{32}	X_{33}	X_{34}	UA_B
B	X_{41}	X_{42}	X_{43}	X_{44}	UA_A
NC	X_{51}	X_{52}	X_{53}	X_{54}	
PA	PA_V	PA_W	PA_B	PA_A	

Each $X_{i,j}$ represents the number of pixels of a given class (column label) classified as the row label, so that their sum represents the total number (N) of control pixels. Consequently, the percentages of correctly (CC) and erroneously (EC) classified pixels are given, respectively, by:

$$CC = \sum_{i=1}^4 X_{i,i} / N \quad EC = \sum_{i=1}^4 \sum_{j=1, j \neq i}^5 X_{i,j} / N$$

UA and PA are defined as the ratio between the total number of pixels correctly assigned to a class with respect to the total number of pixels assigned or, respectively, belonging to the class:

$$UA_i = \frac{X_{i,i}}{\sum_{j=1}^4 X_{i,j}} \quad PA_i = \frac{X_{i,i}}{\sum_{j=1}^4 X_{j,i}}$$

Finally, we used as a global accuracy index the Cohen's K coefficient (Rosenfield and Fitzpatrick-Lins, 1986), defined as:

$$K = \frac{N * \sum_{i=1}^4 X_{i,i} - S}{N^2 - S}; \quad S = \sum_{i=1}^4 \left(\sum_{j=1}^4 X_{i,j} * \sum_{j=1}^4 X_{j,i} \right)$$

In short, while UA and PA make a survey on the behaviours of different classes, K and percentage of correctly classified pixels represent in a general way the performance of each algorithm.

3.3 - Quantitative comparison of algorithms

The output is constituted by an image with each pixel assigned to one of the above classes or, with the exception of C4.5, let unclassified (somehow a better solution than a classification error). In our comparative analysis we took into great attention UA and K . The first was used to evaluate which classes reveal classification problems, the latter to give a comprehensive evaluation of classification performance.

Algorithms were compared on three datasets: the first one (D1) using only the four multi-spectral bands ("red", "green", "blue" and "near IR"); while in the second dataset (D2) the NDVI index for each pixel is added, and the last dataset (D3) uses the previous five features plus the DTM and its gradient values.

The dataset and the algorithm used are appended to the name of each classification test. For example, L0-D1-A means test L0 on dataset D1 using the Adaboost algorithm. For all tests the number of control pixels is always $N=24393$.

In the following tables we report the confusion matrix values for the most significant classification tests. Below each table the performance measures defined in the previous section are reported.

Table 1 and Table 2 report the results of two tests performed using the Adaboost algorithm with the dataset D1 and D3, respectively. Their comparison shows how, despite L0-D3-A uses 7 features versus the 4 features of L0-D1-A, it gets lower CC and K values. While this could be explained by the fact that the DTM and its gradient values could be imprecise because they do not consider artificial structures, it is more difficult to explain why using the dataset D2 with the NDVI index in addition to the 4 multi-spectral bands furnishes a similar result. The same behaviour occurs also the C4.5 algorithm, while the SVM algorithm generally gets, with respect to D1, greater K but lower CC with D2, and very lower K and CC with D3.

Table 3 and Table 4 report the results of the two best performing tests using C4.5 and SVM, respectively.

Figure 4 reports the classification results of the whole case study area using the Adaboost algorithm, test L0-D1-A, while in Figure 2 a zoomed part of it, near a small harbour, is shown. The interpretation of the image is the following: V=green, A=orange, W=blue, B=grey and NC pixels=white.

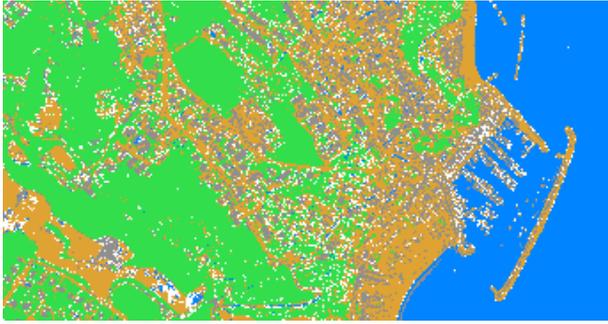


Figure 2. Portion of classification results for test L0-D1-A near a small harbour: V=green, A=orange, W=blue and B=grey, NC=white.

	V	A	W	B	UA
V	9362	4	3	9	99,83%
A	0	1320	2	347	79,09%
W	2	6	11043	23	99,72%
B	3	584	0	1543	72,44%
NC	10	96	7	29	
PA	99,84%	65,67%	99,89%	79,09%	

CC=95,39%; EC=4,61%; NC=0,58%; K=94,62%

Table 1. Confusion matrix and indexes for test L0-D1-A

	V	A	W	B	UA
V	9343	4	0	22	99,72%
A	1	823	2	238	77,35%
W	2	10	11045	12	99,78%
B	5	1060	0	1548	59,24%
NC	29	113	8	131	
PA	99,61%	40,95%	99,91%	79,34%	

CC=93,29%; EC=6,71%; NC=1,15%; K=89,43%

Table 2. Confusion matrix and indexes for test L0-D3-A

	V	A	W	B	UA
V	9333	37	0	31	99,28%
A	0	1243	3	300	80,40%
W	2	14	11051	0	99,86%
B	42	716	1	1620	68,10%
NC	0	0	0	0	
PA	99,53%	61,84%	99,96%	83,03%	

CC=95,30%; EC=4,70%; NC=0,00%; K=93,79%

Table 3. Confusion matrix and indexes for test L0-D1-C

	V	A	W	B	UA
V	9304	5	0	17	99,76%
A	0	1393	5	344	79,97%
W	36	3	11050	0	99,65%
B	37	609	0	1590	71,11%
NC	0	0	0	0	
PA	99,22%	69,30%	99,96%	81,50%	

CC=95,67%; EC=4,33%; NC=0,00%; K=94,25%

Table 4. Confusion matrix and indexes for test L1-D1-S

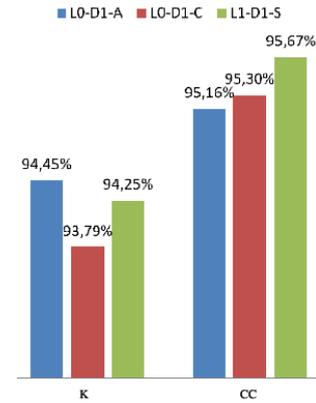


Figure 3. Cohen's coefficient (K) and percentages of correctly classified pixels (CC) in the test with best CC for each algorithm (A=Adaboost, C=C4.5, S=SVM).

4. DISCUSSION AND CONCLUSIONS

The comparison of the results of three automatic classification algorithms (C4.5, SVM and AdaBoost) over different datasets has been presented. The comparison has been performed both qualitatively (photo-interpretation by the superimposition of classification results to an RGB or panchromatic image) and quantitatively (using measures derived from the confusion matrix).

Results demonstrate the suitability of supervised classifiers for high resolution land cover classification. In particular, taking the best performing tests of each algorithm the performances are comparable (see Figure 3). However, the presence of not classified data constitutes a good quality of the two probabilistic approaches; usually in the classification literature this kind of result is considered better than false and positive results and usually not classified classes data are then disambiguated using a second level classifier (different from the first one) mixed with rule based approaches

In conclusion, even in presence of very small training sets the proposed approaches work fine; so that we are now exploring the use of more classes, that is at the second level of the CORINE legend, and an optimal distribution of the samples in the training set.

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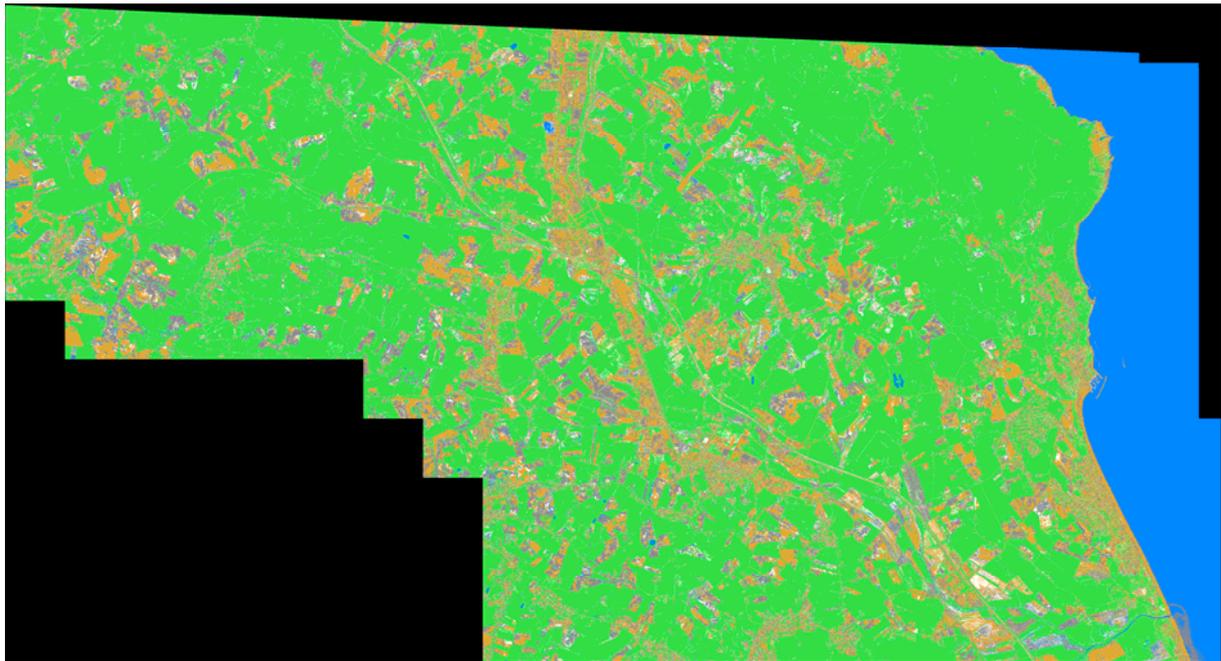


Figure 4. Classification results of the whole case-study area using the Adaboost algorithm: V=green, A=orange, W=blue, B=grey, and NC= white.

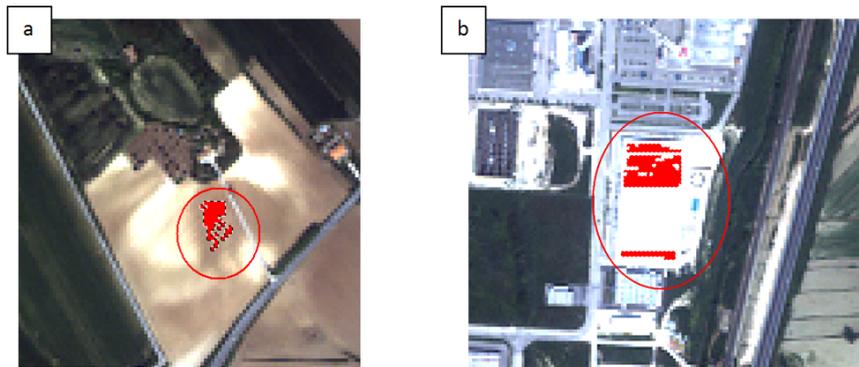


Figure 5. Typical classification errors due to a great similarity between artificial cover and bare soil classes: the red pixels inside the circle are erroneously classified as an artificial cover in image (a) on the left, and as bare soil in image (b) on the right.

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